Making < cinnabar > : Kant on Made A Posteriori Concepts

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KANT ON MADE A POSTERIORI CONCEPTS

by
Sophie Cote

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ABSTRACT

MAKING <CINNABAR>:
KANT ON MADE A POSTERIORI CONCEPTS

by
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The University of Wisconsin-Milwaukee, 2017
Under the Supervision of Professor William Bristow

The topic of this paper is Kant’s distinction between given and made concepts. A made concept is ‘created by us arbitrarily’, while a given concept is ‘produced either through the nature of our understanding or through experience’ (24:131). Kant’s most frequent examples of made concepts are mathematical concepts, such as <triangle>. But mathematical concepts exemplify just one kind of made concepts, namely made a priori concepts. Concepts can also be made a posteriori. The question ‘What is a made a posteriori concept?’ has received little attention. The purpose of this paper is to address this question. I argue that made a posteriori concepts are representations of real essences. As such made a posteriori concepts serve to explain—or grant ‘insight’ into the causes of—observable properties of objects. I show further that made a posteriori concepts are not abstracted from experience. Rather, they are posited as hypotheses in the course of scientific investigation and are for this reason ‘created by us arbitrarily’. Hypotheses are justified by their explanatory power in relation to observable properties of objects and are for this reason a posteriori. In closing I suggest that my reading helps account for the connection between making a concept and making an object which Kant draws, not just in mathematics, but also in the empirical sciences.
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Introduction

The topic of this paper is Kant’s distinction between given and made concepts. A made concept is ‘created by us arbitrarily’, while a given concept is ‘produced either through the nature of our understanding or through experience’ (24:131). Kant’s most frequent examples of made concepts are mathematical concepts, such as <triangle>. For this reason, the distinction has figured prominently in discussions of Kant’s philosophy of mathematics. But mathematical concepts exemplify just one kind of made concepts, namely made a priori concepts. Concepts can also be made a posteriori. The question ‘What is a made a posteriori concept?’ has received little attention. The purpose of this paper is to address this question.

The distinction between given and made concepts is central to Kant’s philosophy of science. Kant takes Newton to have shown that mere observation cannot yield scientific knowledge of the natural world. Instead, the given representations obtained from observation must be ordered by made concepts; only then can ‘the agreement among appearances ... count as laws’ (Bxiii). Made a priori, or mathematical, concepts order the observations of physics. Do made a posteriori concepts fulfill an analogous function? In the literature, all authors deny that they do. I show that this is a mistake, which rests on various incorrect answers to the question ‘What is a made a posteriori concept?’ I argue that made a posteriori concepts are hypothetical representations of essences. As a result, I suggest that made a posteriori concepts order the observations of chemistry.

Here is the plan for the paper: To begin, I say more on the distinction between given and made concepts, and present Kant’s examples of made a posteriori concepts ($1.1-1.2$). I then refute available accounts, with an eye to undermining the claim that made a posteriori concepts are inconsequential to Kant’s philosophy of science ($2.1-2.2$). This makes room for my own account, which I spend the bulk of the paper defending. I argue that made a posteriori concepts grant insight into...

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1. References to the Critique of Pure Reason are to the A and B pagination of the first and second editions. References to the Reflexionen are by numbers. All other references are to the volume and page of the Gesammelte Schriften (Kant 1900). I follow the Cambridge translations where available (Kant 1992, 1997, 1998, 2003, 2004, 2005, 2012). Translations are otherwise my own, and I give the German in an appendix.

things by explaining the causes of their properties. In other words, made *a posteriori* concepts are representations of essences (§3.1-3.3). Next, I propose that made *a posteriori* concepts are ‘created arbitrarily’ because they are scientific hypotheses (§3.4-3.5). In closing, I substantiate my reading by showing that it accounts for three of Kant’s remarks on methodology in chemistry (§4).

1 Two preliminaries

1.1 The distinction between given and made concepts

According to Kant, concepts are either given or made. Given and made concepts do not differ in form. *All* concepts apply to potentially many objects, so all concepts are general in form (9:91). What’s more, we confer generality to our representations, and thus ‘the form of a concept ... is always made’ (9:93).\(^3\) Given and made concepts differ rather in what determines their content. On Kant’s view, each concept is composed of various ‘marks’, which are both predicates and properties of objects.\(^4\) The content of a concept is the marks that make it up. For example, the content of <octagon> is <figure> and <eight sides> (24:254). (I indicate concepts in angle brackets.)

All given concepts are formed tacitly. Given *a posteriori* concepts are ‘given to us through experience’ (24:914). Experience consists in ordered sensory impressions (A1=B1); that is, experience presents us perceptually with objects (Bxvii). At first blush, then, given *a posteriori* concepts are determined only by past perceptual encounters with objects.\(^5\) Examples include the concepts of a horse, a sheep (24:253) and water as ‘a fluid body’ (24:914). What the class of given *a posteriori* concepts encompasses is at issue, so I defer a more meticulous analysis. Given *a priori* concepts are determined by ‘the nature of our understanding’ (24:131). The understanding is our capacity for thought; it conceptually structures experience (A19=B33). Given *a priori* concepts are preconditions on our experiencing the world as we do. These include <quantity> and <cause> (24:756).

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4. In Kant’s words: ‘A mark is that in a thing which constitutes a part of the cognition of it, or ... a partial representation, insofar as it is considered as ground of cognition of the whole representation’ (9:58). The move from property (‘that in the thing’) to predicate (‘a partial representation’) is of course puzzling. For discussion, see Smit 2000, 247-8.

5. I borrow the phrase from Rosenberg (2005, 33).
Made concepts, in contrast, are ‘created by us arbitrarily [willkürlich]’ (24:132). Following the eighteenth-century usage, ‘arbitrarily’ means electively, and not at random. As Kant clarifies elsewhere, made concepts are determined only by our own volition, or power of choice [Willkür] (24:914). In practice, made concepts originate in something like a stipulative definition, or ‘arbitrary synthesis’ (24:918). (I have some misgivings about the talk of stipulation, which I explain in due course.) Mathematical concepts, according to Kant, are made in this sense: ‘[w]hatever the concept of cone may ordinarily signify, in mathematics the concept is the product of the arbitrary representation of a right-angled triangle which is rotated on one of its sides’ (2:276).

Mathematical concepts are made a priori (24:915). But concepts can also be made a posteriori: ‘[a]rbitrary concepts can be made both a priori and a posteriori’ (24:918). I pause to say a word on Kant’s usage of the phrase ‘a posteriori’. Setting difficulties aside, a concept is a posteriori if its content is answerable to experience (B2). Now, it is not immediately obvious how a concept can be both made—its content determined only by my own volition—and a posteriori—its content answerable to experience. Kant offers just two examples, and both are drawn from chemistry: ‘the concept of the essence of gold’ and ‘the nature of metal’ (24:132; 24:914).

I have steered clear of the term ‘empirical’. I believe that Kant does not use ‘empirical’ and ‘a posteriori’ interchangeably, at least in the context relevant to my topic. Here my reading departs from others I consider. In order not to beg any questions, I avoid the term ‘empirical’ until §3. Last, and by way of summary, here are Kant’s examples again:

<table>
<thead>
<tr>
<th></th>
<th>a priori</th>
<th>a posteriori</th>
</tr>
</thead>
<tbody>
<tr>
<td>given</td>
<td>&lt;quantity&gt;</td>
<td>&lt;horse&gt;</td>
</tr>
<tr>
<td>made</td>
<td>&lt;triangle&gt;</td>
<td>&lt;essence of gold = ...&gt;</td>
</tr>
</tbody>
</table>

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6. *Willkür* is also, and primarily, the capacity to decide how to act. Kant quotes Juvenal’s *sic volo, sic iubeo* [thus I will, thus I command] to describe both the autonomous law-givingness of practical reason (5:31) and the arbitrariness of mathematics: ‘The mathematician says in his definition: *sic volo, sic iubeo* [sic]’ (*Reflexion* 2930, my translation).

7. I assume with other interpreters that what is made is the concept we acquire of the essence, not the one composed strictly of the two marks <essence> and <of gold>. In the table below, I resort to an ellipsis: <essence of gold = ...>. 
1.2 Kant’s examples of made a posteriori concepts

The scientific character of Kant’s examples of made a posteriori concepts has not generally been noted. On the contrary, it has been claimed that Kant puts forward a non-scientific example. The purported example is found in the Critique, where Kant mentions the concept <ship’s clock> and says it is made (A729=B757). A ship’s clock is a clock precise enough for the computation of longitude. Such an instrument did not exist until 1773, and before then the concept applied to a merely fictive object (Kant 1998, 752 n10). Many have speculated that <ship’s clock> is a made a posteriori concept (Callanan 2014, 589; Dunlop 2012, 96; Heis forthcoming, 12; Paton 1936, 197).

Two existing accounts of made a posteriori concepts are premised on the conjecture that <ship’s clock> is made a posteriori. Heis and Paton propose that a concept is made a posteriori if the concept is stipulated and applies, or would apply, to physical objects. Besides <ship’s clock>, alleged examples include <swampman> (Heis 2007, 149) and <centaur> (Paton 1936, 197). Messina and Stang suggest that a concept is made a posteriori if the concept applies to a merely conventional kind, i.e. not a natural kind. Alleged examples include <table> (Messina 2015, 429) and <weed> (Stang 2016, 237). The two readings are sketched in passing. Perhaps this betrays the widespread assumption that made a posteriori concepts are inconsequential to Kant’s philosophy of science. If either of these readings is correct, the assumption is of course quite justified.

But <ship’s clock> is not made a posteriori. In a lecture contemporaneous with the Critique, Kant writes: ‘we can also have a concept a priori factitus [or made] ... . This is how it happens with someone who invents a new instrument’ (24:915). That is, the concepts of invented instruments are made a priori. The context rules out any confusion, as Kant is explicitly contrasting made a priori and a posteriori concepts. <ship’s clock> is the concept of an invented instrument, so we must infer that it is made a priori. Therefore the example does not lend support to either reading; on the contrary, it constitutes a counter-example to both. In conclusion, Kant’s only examples of made a posteriori concepts (<essence of gold> and <nature of metal>) are scientific concepts.

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8. Adickes dates the Vienna Logic to 1780-1. This dating is matter of dispute, however. See Forster (2012, 490-3).
9. Only Nunez advances the correct diagnosis, but without textual evidence (2014, 653 n10).
2 Making room for a new reading

I now present and refute the third available reading of made a posteriori concepts, which I dub the ‘amplification reading’. This makes room for my own reading, which I defend in the next section.

2.1 The amplification reading

The third extant reading does justice to Kant’s own examples. Indeed, the reading takes as its starting point the dependence of made a posteriori concepts on scientific investigation. Kant writes:

I have a piece of metal[,] that is always given a posteriori, not made. If I want to have a distinct concept of it, however, then I have to test the metal for all its properties ... the nature of metal is thus a concept made a posteriori. (24:914)

That is, a given a posteriori concept precedes investigation, while a made a posteriori concept results from it (‘I have to test the metal’). If so, perhaps a given a posteriori concept is the concept I first possess of the object, or a conceptual stereotype that allows me to so much as recognize the object. Investigation takes place when I decide to add to my concept by acquiring further information about the thing. A concept that contains a mark obtained from investigation is made a posteriori. Call this the ‘amplification reading’. This reading is defended by Dunlop (2012), Nunez (2014) and Young (1992; 1994).10

If made a posteriori concepts are characteristically scientific, it is because science is the main avenue for ‘conscious investigation’ (Young 1994, 338). But given and made a posteriori concepts do not constitute radically different kinds of representations. Both are empirical concepts (Dunlop 2012, 94), because both are formed from marks obtained through observation. Kant calls

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10. The main text presents a neutral gloss on the view. Let me briefly address the variants.

(i) As noted in §1.2, Dunlop takes <ship’s clock> to be made a posteriori. So far as I can tell, made a posteriori concepts are believed to form a disparate class (2012, 94, 96, 117 n19).

(ii) For Nunez, made a posteriori concepts are ‘arrive[d] at through hypothesis ... which we test against appearances through observation’ (Nunez 2014, 653 n10). Perhaps the emphasis on hypotheses sets Nunez’s proposal apart—and closer to the one I am about to defend. Nevertheless, I discuss a disagreement in footnote 29.
‘empirical synthesis’ the process of adding marks to a concept through observation, and concepts obtained in this way are ‘made empirically’ (24:918). On the amplification reading, made a posteriori concepts are made by empirical synthesis, or made empirically. As proponents of this reading point out (Dunlop 2012, 95; Young 1992, 338 fn16), §102 of the Jäsche Logic seems to offer conclusive evidence in support of this reading: ‘the synthesis of concepts that are made ... is either that of exposition (of appearances) or [a priori]. ... the former ... are made empirically’ (9:141).

Authors diverge in how they explain the arbitrariness of made a posteriori concepts. Perhaps the content of a made a posteriori concept is contingent upon our choice of experiment; or perhaps our investigation of the thing must ‘begin as it were, by legislating the conditions a thing must satisfy to qualify as an instance of the concept in question’ (e.g. let’s only call ‘water’ what has a hydrogen-1 isotope) (Young 1992, 111). In either case, the arbitrariness of made a posteriori concepts consists in the contingency of their content, and the ‘madeness’ of made a posteriori concepts is of little philosophical interest.

2.2 Two objections to the amplification reading

The dependence of made a posteriori concepts on investigation is central to Kant’s view. My first objection, however, is that the reading mischaracterizes this dependence. Again, the suggestion is that a concept is made a posteriori if it contains at least one mark obtained from empirical investigation. But in a previously cited passage Kant makes a different point. To possess a made a posteriori concept, I must test the thing ‘for all its properties’ (24:914, my emphasis). Testing for just one property does not yield a made a posteriori concept. This conclusion entails further that the arbitrariness of made a posteriori concepts cannot consist in the contingency of their content. If I must test the thing of all its properties, then my decision to first investigate a certain property, or to treat it as characteristic of the kind, does not influence the content of my concept.

Perhaps the passage should not be read literally. Indeed Kant often asserts that we ‘cannot possibly examine an object regarding all its properties’ (Kant 1992, 409). If read literally, the passage imposes a condition on made a posteriori concepts that simply cannot be met; yet there
exist made \textit{a posteriori} concepts. This contradiction is reason not to read the passage literally. If testing a thing for all its properties is not a condition on our possessing a made \textit{a posteriori} concept, maybe it is one goal of scientific inquiry. Yet a \textit{Reflexion} of the same period rules out this non-literal reading. A made concept of an object of experience is ‘only possible if’ the object is ‘grasped in all its determinations’ (\textit{Reflexion} 5221, my translation). For present purposes, a determination just is a property (24:931; A598=B626). This \textit{Reflexion} reaffirms that testing for just one property does not yield a made \textit{a posteriori} concept. The amplification reading is forced to disregard these passages. I will shortly defend a solution to the tension between Kant’s various claims that is interpretively more satisfying and philosophically more interesting.

My second objection is that the amplification reading is incompatible with the very text—the \textit{Jäsche Logic}—that is used to motivate it. Recall that on this reading, (i) given and made \textit{a posteriori} concepts are empirical, and (ii) a concept is made \textit{a posteriori} if it is made empirically, or by empirical synthesis. We saw that §102 is evidence in support of (ii). Difficulties arise, however, from the footnote to §102, which reads: ‘all empirical concepts must thus be regarded as concepts that are made, whose synthesis is ... empirical’. Factoring (i) and (ii) into this footnote produces the claim that all given or made \textit{a posteriori} concepts are made \textit{a posteriori}. Yet Kant upholds the distinction between given and made \textit{a posteriori} concepts in the \textit{Jäsche Logic} (9:141), and makes clear that the class of given \textit{a posteriori} concepts is not empty (9:64). Thus, claims (i) and (ii) entail textual contradictions in spite of textual evidence in support of (ii).11

We must weigh the main text of §102 against the rest of the \textit{Jäsche Logic}. I suggest we dismiss whatever evidence §102 offers in support of claim (ii), that is, the claim that made \textit{a posteriori} con-

11. In response to something like this objection, Dunlop writes (2012, 117 fn19):
In \textit{Reflexionen} 2910 and 2914, Kant indicates that all empirical concepts are made in this way [empirically]. But at this stage, he does not seem to recognize \textit{a priori} factitious concepts as different in kind from both empirical and “rational” \textit{(a priori)} given concepts, which suggests that the given/made distinction has not yet become an axis of classification distinct from the rational/empirical one. ... §102 of the \textit{Jäsche Logic} can thus be taken to address the inadequacy of the earlier taxonomy.

But \textit{Reflexion} 2910 is dated by Adickes to 1776-1778 or 1790-1792, and the distinction between given and made concepts—each \textit{a priori} or \textit{a posteriori}—appears as soon as the \textit{Blomberg Logic} of the early 1770’s. At any rate, and as I show in the main text, the same tension is found within the confines of §102.
cepts are made empirically, or by empirical synthesis. What motivates this interpretive decision are the following two considerations. First, the footnote to §102 indicates that concepts made empirically are ‘not arbitrary, however’. There is no reason, besides §102, to suspect that Kant gave up the view that made a posteriori concepts are arbitrary. Second, Kant elsewhere contrasts the arbitrary synthesis of made a posteriori concepts with the empirical synthesis of empirical concepts (24:918). Thus the evidence for (ii) is flawed, and I rule against the amplification reading.

3 Sketching a new reading

I now defend an alternative reading. I hope to demonstrate that the connection between made a posteriori concepts and scientific investigation runs deeper than existing interpretations suggest.

3.1 Made concepts and superordination

I begin to build my case by noting the link between made a posteriori concepts and ‘having insight’. The latter is a term of art. Kant follows the rationalist tradition in identifying seven ways we can apprehend objects, from representing [sich etwas vorstellen] to comprehending [comprehen-dere, begreifen]. In an overlooked passage of the Blomberg Logic, Kant discusses made concepts in relation to the sixth and penultimate degree, having insight [einssehen] (24:132-5). The concept of the essence of gold, Kant seems to suggest, grants insight into gold. This connection, between a made a posteriori concept and having insight, is the one I wish to expound and build on.

To have insight into a thing, Kant indicates in the passage under discussion, is to represent a thing ‘through mediate marks, [to] infer, then, and thus search for a nota notae, a mark of the mark’ (24:135). This gloss poses an interpretative difficulty. Kant departs from the rationalist tradition in distinguishing between two sorts of mediate marks, namely, logically and really mediate marks. It is not clear from Kant’s gloss which sort of mediate marks is required to have insight.

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12. Paton also alleges ‘some confusion,’ ‘perhaps due to the notetaker’ (1936, 197 fn4).
13. All concepts are mediate representations, because they apply to objects via the marks they contain (A68=B93). But concepts may be mediate or immediate marks of a thing. Cf. Longuenesse (2001, 88 fn15).
Here is a general characterization of mediate marks. Consider an object \( x \) and two distinct marks \( M_1 \) and \( M_2 \) correctly predicated of \( x \). If \( M_2 \) is superordinate to \( M_1 \), then \( M_2 \) is a mediate mark of \( x \). Conversely, if \( M_1 \) is superordinate to no mark of \( x \), then \( M_1 \) is an immediate mark of \( x \) (24:108). The explanatory burden is now on superordination. (By 'superordination' I mean the inverse relation to subordination. Talking of superordination enables me to keep the focus on mediate marks.) Superordination is a deductive relation amongst marks. It comes in two kinds (2:260), corresponding to the two aforementioned sorts of mediate marks.

Logical superordination is a matter of conceptual containment. \( M_2 \) is logically superordinate to \( M_1 \) if \( M_1 \) contains \( M_2 \) as a constituent (24:108). For example, \(<\text{man}>\) is logically superordinate to \(<\text{bachelor}>\). Imagine I recognize Tim as a bachelor and affix the mark \(<\text{bachelor}>\) to Tim. \(<\text{man}>\) is logically superordinate to \(<\text{bachelor}>\), so \(<\text{man}>\) is a logically mediate mark of Tim.

Real superordination is a matter of causal entailment.\(^{14}\) \( M_2 \) is really superordinate to \( M_1 \) if \( M_2 \) is the cause of \( M_1 \) (24:260). For example, \(<\text{was chilled}>\) is really superordinate to \(<\text{catches a cold}>\) (28:403). Consider then sick Tim, who possesses the mark \(<\text{catches a cold}>\). \(<\text{was chilled}>\) is really superordinate to \(<\text{catches a cold}>\), so \(<\text{was chilled}>\) is a really mediate mark of sick Tim.

Back to having insight. Recall that to have insight into a thing is to 'cognize [the thing] through mediate marks'. But which sort, if not both? On two occasions, Kant suggests that having insight requires cognizing the thing through really mediate marks. '[B]y means of analysis', Kant writes, 'I cannot have insight' (2:370);\(^{15}\) analysis just is the cognition of logically superordinate marks (9:142). Second, Kant once glosses having insight as knowing causes (24:51). I conclude that to have insight into a thing I must cognize at least one of the thing's really mediate marks.\(^{16}\)

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14. I assume that real superordination is only causal. See 24:260: ‘Real [super]ordination ... consists in the fact that’ marks ‘cohere as causes and effects’. In spite of like passages, Stang perceives a distinction between causal and non-causal real superordination, and contends that essential and non-essential marks—which are at issue in this paper—stand in a relation of non-causal real superordination (2016, 209). I believe this much is mistaken, for Kant indicates that essential marks are causes (24:113). At any rate, the precise nature of the relation plays no role in my argument.

15. The Cambridge edition incorrectly renders 'einsesehen' as 'understanding', and obscures this point (2003, 356).

16. Two remarks on this conclusion: (i) I acknowledge that most often Kant’s glosses are ambiguous (24:152, 24:539, 24:730, 24:840, 28:24). Still, there is no doubt that insight into at least empirical objects requires more than logically mediate marks. This claim fuels Kant’s objections to the Leibnizian-Wolffian program. (ii) To have insight is also to cognize a priori (24:133). I believe Kant intends here only the Leibnizian sense of prioricity as cognition through mediate marks (cf. Smit 2009; Stang 2016, 23)
I noted that Kant suggests a connection between made *a posteriori* concepts and having insight. In light of my discussion of ‘having insight’, I hypothesize that a concept is made *a posteriori* if it is made up of some of the really mediate marks of a thing. I now substantiate this hypothesis.

Evidence for this hypothesis can be adduced from Kant’s own examples. Recall that the concepts of the essence of gold and the nature of metal are made *a posteriori*. ‘Nature’ and ‘essence’ are synonyms (24:840).¹⁷ Now, Kant defines ‘essence’ as ‘the first ... ground of all that which belongs to the thing itself’ (29:820);¹⁸ a ground is nothing other than a mediate mark. Furthermore, Kant elsewhere clarifies that the essence contains the really mediate marks of the thing (28:49). In summary, the essence of a thing is made up of the really mediate marks most superordinate to ‘all that which belongs to the thing itself’.

Let us now ask what ‘belongs to the thing itself’. On an intuitive picture, the essence of a thing causes only its necessary properties. The essence of gold plausibly causes its conductivity and malleability, but not that it is valued at $37 per gram. This is just Kant’s view. The essence of a thing is the sufficient cause of its *attributa* (or ‘Eigenschaften’) (8:229, translated in Kant 1973, 141). Equivalently, the *attributa* are the consequences of the thing’s essence. As Kant makes plain, *attributa* just are ‘necessary marks’ (9:113).

To sum up, here is what I have just shown. Kant’s own examples suggest that a concept is made *a posteriori* if it explains the causes of the thing’s properties. That is, a concept is made *a posteriori* if it contains the thing’s really mediate marks. For this reason, made *a posteriori* concepts grant insight into the thing.

3.2 Given concepts and coordination

I have not yet shown that the connection to having insight is characteristic of made concepts. I now argue that given *a posteriori* concepts only grant the fifth and immediately lower degree of cognition, understanding. (Understanding should not be confused with the understanding

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¹⁷. Or close enough, and at least for concrete objects (Messina, forthcoming, 16; Oberst, n.d.; Stang 2016, 238–239).

¹⁸. I omit (with an ellipsis) the qualification, ‘inner’ ground. An object is also determined by ‘outer’ grounds, which do not however figure in its essence (28:52). These include the conditions on sensible experience.
[der Verstand], which is our capacity for thought. All concepts originate in the understanding.) In contrast to having insight, to understand is to represent a thing ‘through immediate marks’ (24:132). I proceed in two steps. I show that: (i) all given a posteriori concepts are abstracted from experience, and (ii) all concepts abstracted from experience contain only really immediate marks.

To abstract a concept from experience is roughly to single out the sensible marks common to all known instances of the kind (24:126). The shortest argument to (i) is simply to point out that at 24:253 Kant writes: ‘[a]ll conceptus a posteriori dati [given a posteriori concepts] are abstracted ab experientia [from experience]’. A more roundabout argument is available, which relies on Kant’s technical use of the term ‘empirical’. First, a concept is empirical if and only if it is abstracted from experience (24:905). Second, a given a posteriori concept just is an empirical concept. Kant lists the two as synonyms at 24:756 and 24:918. Again we must conclude that all given a posteriori concepts are abstracted from experience.

I now turn to (ii), viz. the claim that all concepts abstracted from experience contain only really immediate marks. First, note that two immediate marks of a thing cannot stand in a relation of superordination to one another. If a mark is superordinate to another, it is mediate relative to the thing. Marks that are not superordinate are coordinate. Kant thinks that ‘with empirical cognitions, there is not a series of [super]ordinate, but only of coordinate’ marks (24:155). Equivalently, experience only provides immediate marks (2:294), and one ‘can never experience a cause’ as a cause (24:752). Thus relations of real superordination are not abstracted from experience.

I pause to acknowledge a difficulty. If experience only provides immediate marks, then relations of logical superordination are not abstracted from experience either. This is indeed Kant’s view (see A305=B362). Relations of logical superordination arise only through reflection on what is common to various concepts. For example, and very roughly, reflection on <rabbit>, <cat>, <horse> etc. yields the superordinate concept <mammal>. It may be objected that this aspect of Kant’s view is at odds with the reading I defend. I have argued that all empirical concepts are abstracted from experience. Yet, the objection goes, we routinely deduce logically superordinate marks. For example, we may deduce from the fact that Tim is a bachelor that he is a man and
therefore mortal. Such a logical deduction follows relations of logical superordination that are not abstracted from experience. Perhaps my reading entails the implausible claim that the concept I possess after the logical deduction (e.g. \(<\text{Tim} = \text{bachelor, mortal}>\)) is not empirical.

I grant that this would be an implausible claim. But such a claim is not entailed by my reading. For Kant, logical deduction serves to clarify the content of my concept, but not to change it in any way. The mark \(<\text{mortal}>\) ‘is already there’ as soon as I recognize Tim as a bachelor (24:131). Of course, this mark may be only ‘obscure[ly]’ thought (24:130). Logical deduction serves precisely to clarify the content of my concept. But logical inference does not amplify the concept I possess of the thing, so I ‘do not cognize any more in a thing than [I] have already thought in it previously’ (24:131). In conclusion, the content of given \(a \text{ posteriori}\) concepts is wholly abstracted from experience. In contrast, made \(a \text{ posteriori}\) concepts contain really mediate marks of the thing, which do amplify my knowledge of the thing and are not abstracted from experience. Thus a clear distinction between given and made \(a \text{ posteriori}\) concepts can be maintained.

3.3 \textit{Made \(a \text{ posteriori}\) concepts result from investigation}

Let us then ask how made \(a \text{ posteriori}\) concepts arise, or—what is the same—how really mediate marks are obtained. Kant’s answer, in short, is that really mediate marks (i.e. the \textit{relata} of causal relations) are inferred on the basis of experience (28:24; 24:237). ‘[T]here is a sun in the heavens, the barometer has fallen or risen’, ‘gold does not rust’ (24:231)—these judgments ascribe immediate marks to their subjects and are evident from perceptual experience (Vanzo, forthcoming, 23). The cause of these various marks are only grasped by careful empirical investigation and scientific inference (24:231). The same is true of the causes of a thing’s properties:

To understand something is far easier than to have insight into something, for in the first case it is only necessary that I coordinate the marks of a thing, but in the other case I must [super]ordinate them. To understand what gold is I need nothing more than to know the properties \(\text{[Eigenschaften]}\) of this metal, that it is, e.g., ductile, yellow,
heavier than others, etc., that it does not rust. But to have insight into what gold is I must investigate one of its marks in particular and abstract from it its ground. E.g., why it does not rust, why is it ductile, heavier than others. (24:135)

Inferring essential marks poses specific difficulties.¹⁹ For most of his writing years, Kant endorses the phlogistic theory of the German chemist Georg Stahl. For Stahl, and for Kant, the essences of things consist in chemical elements that are in principle unobservable (A646=B674; 29:162). Therefore made a posteriori concepts are made up of marks that are in principle unobservable. By way of illustration, the essence of cinnabar, for Stahl, is \( (S+P+M)+M+[(W+S)+P]+(W+S) \), where \( S = \) salt, \( P = \) phlogiston, \( M = \) mercury—three unobservable elements—and \( W = \) water—a vehicle. On my reading, \( \langle \text{essence of cinnabar} = (S+P+M)+M+[(W+S)+P]+(W+S) \rangle \) is a made a posteriori concept. In contrast, \( \langle \text{cinnabar} = \text{red, heavy, mineral} \rangle \) is a given a posteriori concept. (Given a posteriori concepts are not limited to the ways things look—or sound, smell, taste, and feel. They also feature dispositional properties, e.g. \( \langle \text{does not rust} \rangle \), and what Kant dubs negative and comparative marks, e.g. \( \langle \text{without odor} \rangle \) and \( \langle 14 \text{ times lighter than quicksilver} \rangle \) (24:118).)

I now consider one objection. That made a posteriori concepts are representations of essences is central to my account. Yet Kant often insists that the ‘essence of things is inscrutable to us’ (28:557). If so, we may question the plausibility of my reading. In response to this objection, I note first that Kant sometimes breaks with this skepticism concerning our ability to cognize essences. When he does, his examples are drawn from chemistry: ‘“The essence of the defined thing”: This, we cannot always find, but in brass it can be found’ (Reflection 2988, my translation). (Stahl discusses the essence of brass in his main work, the Philosophical Principles of Universal Chemistry (1730, 335).) Second, the 28:557 passage continues: the ‘essence of things is inscrutable to us, although we cognize many essential aspects’.²⁰ That is, our knowledge of essences is perhaps partial and fallible, yet we may still cognize some essential marks of objects. Importantly, Kant explains that we come to know these essential marks ‘bit by bit in experience’ by ‘infer[ring] ...
from the properties known to us’ (28:557). Finally, I point out that many have recently argued that for Kant all chemical laws are derived from, or grounded in, the essences of things.\textsuperscript{21} If this is right, it is likely that our chemical theories will need to feature made \textit{a posteriori} concepts, i.e. representations of essences.

To sum up: Given \textit{a posteriori} concepts are abstracted from experience; made \textit{a posteriori} concepts result from scientific investigation and inference. If I am right, only the latter possess explanatory power. This is just what Kant suggests: ‘[w]ith all empirical concepts there is only a description’ (24:270), and ‘[i]n all description one seeks more to understand the thing than to have insight into it’ (24:109). Description contrasts with explanation, where ‘one seeks again on the contrary more to have insight into the thing than to understand it’ (24:109).

3.4 ‘Arbitrary’ and ‘\textit{a posteriori}’, redux

In §1.1. I presented Kant’s characterization of made concepts. All made concepts are ‘created by us arbitrarily’ (24:132). I have not yet explained in what sense made \textit{a posteriori} concepts are created arbitrarily. In addition, I noted that it is not immediately obvious how a concept can be both made—its content determined only by my own volition—and \textit{a posteriori}—its content answerable to experience. In this subsection, I argue that (i) all hypotheses are arbitrary, and (ii) all made \textit{a posteriori} concepts are hypotheses. Finally, I suggest that the content of made \textit{a posteriori} concepts is answerable to experience because hypotheses must be justified by experience.

First is the claim that (i) all hypotheses are arbitrary. Kant defines a hypothesis as ‘something [that] is accepted as a ground from which I can have insight into the sufficient ground of given consequences’ (24:886). The ground which is put forward as a hypothesis, Kant suggests, is constrained but not determined by experience. For this reason, ‘with a hypothesis the consequences are given but the ground is invented’ (24:222). As Kant puts it again in the \textit{Critique}, to hypothesize is ‘to invent’, albeit ‘under the strict oversight of reason’ (A770=B798; see Butts 1961, 155). Kant concludes that the content of all hypotheses is determined by our volition, and ‘all hypotheses are

posited *arbitrarily* (24:221).

I now argue that (ii) made *a posteriori* concepts are hypotheses. Of this paper’s various steps, this claim is supported by the least direct textual evidence. Yet it is not without warrant. Clues can be obtained by tracking Kant’s use of the term ‘fiction’ ('fictio’) and its cognates (notably ‘fictitious’). First, Kant asserts that hypotheses constitute a kind of fiction, apparently because to hypothesize is to invent (24:223-4; 24:262).22 Second, Kant insists that made concepts are fictions (24:133; 24:252; 24:261-2). That both hypotheses and made concepts are fictions does not appear to be a coincidence, for Kant once ends a discussion of made concepts with the contention that ‘hypotheses are of this kind’ (24:262). It is a short step to the conclusion that made *a posteriori* concepts are fictions because they are hypotheses, and one I propose to take. Therefore, made *a posteriori* concepts are ‘created by us arbitrarily’ because they are scientific hypotheses.

I want to underscore in passing the connection between hypotheses and having insight. Again, a hypothesis is ‘something [that] is accepted as a ground from which I can have insight into the sufficient ground of given consequences’ (24:886). If I am right to conclude that made *a posteriori* concepts are hypotheses, then Kant’s definition of hypotheses offers further evidence for the connection between made *a posteriori* concepts and having insight that is central to my reading.

Kant’s discussion of hypotheses also explains in what sense the content of made *a posteriori* concepts is answerable to experience. As we saw, a concept is *a posteriori* if it is answerable to experience. Hypotheses are answerable to experience insofar as they are confirmed by their connection to observable consequences. As Kant puts it, a hypothesis that is ‘confirmed and derived ... through relation to [its] consequences’ is *a posteriori* (24:221). In §1.1 I noted my reluctance to gloss all made concepts as stipulated concepts. We now see why. All made concepts originate in an arbitrary synthesis (24:918). Perhaps in the case of made *a priori* concepts the arbitrary synthesis amounts to a stipulation.23 If so, the concepts’ content depends only on their definition.

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22. Kant occasionally points out that hypotheses are not mere ‘arbitrary inventions’ or ‘mere chimeras’ (A822=B850; 9:85). As the context makes clear, and the passages cited in the main text further establish, these reminders serve only to distinguish hypotheses from unconstrained metaphysical speculation, not to deny that hypotheses are fictions.

and calls for no further justification. But made \textit{a posteriori} concepts are answerable to experience. Here the arbitrary synthesis amounts rather to a positing.

This completes my positive proposal. I have argued that made \textit{a posteriori} concepts are scientific hypotheses concerning the essences of things, and as such grant insight into things.

3.5 \textit{Tying up loose ends}

With my account now firmly in view, I revisit Kant’s claim that a made \textit{a posteriori} concept requires that I test the thing ‘for all its properties’ (§2.2). I opposed this claim to the amplification reading, but it remains unexplained. As we saw, this claim entails a contradiction. Kant holds that we cannot possibly test anything for all its properties; and yet he gives examples of actual made \textit{a posteriori} concepts. My solution to this tension is two-fold. First, I interpret the claim at issue in terms of justification. I have just presented Kant’s claim that hypotheses are confirmed ‘through relation to their consequences’. Kant naturally draws the further conclusion that a hypothesis is fully confirmed if and only if it explains all consequences that are to be explained. To fully justify a hypothesis, then, I must know all consequences that are to be explained.

Second, I underscore that made \textit{a posteriori} concepts are hypotheses concerning the essence of a thing. The essence of a thing is the cause of all the thing’s properties, so ‘to find the real essence [I] must be acquainted with all the marks that belong to the thing ...’. Then [I] must search further for the ground of these’ (24:118). Although testing for all properties is not a condition on my possessing a made \textit{a posteriori} concept, it is a condition on my made \textit{a posteriori} concept being fully justified. My solution requires tweaking Kant’s words. Yet I think it captures an important lesson of Kant’s philosophy of science. Namely, that the explanatory ambition of the empirical sciences is frustrated by the inexhaustible richness of empirical experience.

Next, I want to address the fact that Kant’s own examples of made \textit{a posteriori} concepts are drawn from chemistry. On the amplification reading, any scientific concept is made \textit{a posteriori}, including e.g. descriptions from biology.\textsuperscript{24} This position weakens the link between made \textit{a pos-
In this section, I call attention to three of Kant’s remarks on scientific methodology that I argue give credence to my reading. Consider first:

we see, whether we can also make the concept. E. g. the definition of cinnabar, sublimed Quicksilver and Sulphur give cinnabar: I can then make cinnabar and define it.

(24:660, my translation)

One can define [later addition: explicate] empirical concepts, if one can make the

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25. See the definitions in Boerhaave (1735, 19) and Boyle (1772, II, 474). For recent discussion, see Holmes (1997).
26. More correctly still, the connection is a matter of stipulation: any scientific investigation of natural causes would have constituted chemistry. Textbooks commonly contained sections on vegetals and animals, which discussed anything from the growth of plants to physiological processes and fluids. Indeed, a hugely influential textbook defined chemistry as the ‘science of all natural things’ (Le Febvre 1670, Preface). But the essence of organisms of course remained mysterious, which explains why Kant would have picked instead the example of metals.
27. Definitions proper are exhaustive and precise. A definition is exhaustive if the definitiens contains all the marks that make up the definiendum; it is precise if the definitiens contains no redundant marks. A definition merely expounds if it is either incomplete or imprecise. In the passage above, Kant retains the clause ‘complete exposition’. I conclude that the definition is only imprecise. Imprecision is a negligible flaw (a mistake ... but not an error; 24:269).
object e.g. gypsum, cinnabar, sulphur. A complete exposition of the appearance. (Re-flexion 2964, dated 1776-1789, my translation)

Kant here suggests two connections: (i) between making a concept and making the object; (ii) between making the object and defining it. (The passages contain likely references to Stahl's *Philosophical Principles of Universal Chemistry*. Stahl discusses the elemental composition of gypsum, cinnabar and sulphur in three consecutive sections (1730, 167-84), and gives an identical definition of cinnabar (1730, 167, 173).)

Much in these remarks will surprise readers familiar with Kant’s philosophy of mathematics. The connections between making a concept, making the object, and defining it are a mainstay of Kant’s writings on mathematics. Kant (and certainly interpreters) often suggests that only mathematics can exemplify this connection. This naturally raises the question of whether these unpublished remarks represent Kant’s considered view. I do not wish to investigate this issue here, however. My aim in this section is more limited. I suggest simply that the reading I defend renders these passages intelligible.

The connection between a made *a posteriori* concept and making the object can be explained by my reading. Made *a posteriori* concepts are hypotheses concerning the causal grounds of the properties of the thing. If our hypothesis concerning these causal grounds is adequate, it is plausible that we would be in a position to make the thing. Indeed, the ability to make the thing is evidence of the adequacy of our concept. In this sense, made *a posteriori* concepts are similar to made *a priori*, or mathematical, concepts. This leads us to the link between making an object and defining it. Kant follows Aristotle’s lead in claiming that to define a thing just is to give its essence (9:143). The ability to produce the thing offers evidence that our concept of the essence is adequate, so the making the thing is evidence that our definition of it is correct.

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28. E.g. Heis: ‘Kant was committed to a particularly strong thesis about mathematical concepts and definitions. He believed that possessing a concept, having its definition, and being able to construct instances of it were all coeval abilities.’ (2014, 608).

29. Nunez (2014, 653 fn10) notes the 24:660 passage but resists the conclusions I draw:

    such a definition [of cinnabar], made out of empirical concepts, however, is not a counterexample to Kant’s claim that empirical concepts cannot be defined, because these are technical concepts for making
Kant expands on this connection in the following passage:

Chemistry, which decomposes [or analyses] water, and produces it back ... . Whether I can produce a decomposed concept by synthesis, should be evident from the properties that flow from it. (*Reflexion* 2402, dated 1776-1789, my translation)

This passage is of interest to me for the similarity it bears to one of Kant’s conditions on justified hypotheses. As we saw earlier, Kant contends that a hypothesis is justified only if the consequences that it must explain can be derived from it. Repeatedly, in formulating this condition, Kant uses the phrase ‘flowing from’. A hypothesis is more than a ‘mere chimera’ if and only if ‘[f]rom the assumed ground the consequences ... flow correctly’ (9:85; cf. 24:111; 24:221; 24:746). We may infer that a made *a posteriori* concept is the assumed ground, and the properties of the object, the consequences of that ground. If this is so, the passage provides further evidence that chemical concepts are hypotheses, and thus arbitrary.

Finally, Kant often asserts that ‘we only have insight into what we can make’, and offers chemical examples, such as the dissolution of salt (*Reflexion* 2394, 2398). Insofar as I am right to posit a link between made *a posteriori* concepts and making the object, these passages strengthen the connection to having insight that is central to my reading.³⁰

**Conclusion**

The purpose of this paper was to answer the question ‘What is a made *a posteriori* concept?’. I have argued that a made *a posteriori* concept is a hypothetical representation of a thing’s essence, which grants insight into the thing. In the course of arguing for this conclusion I have demonstrated the things, not the kind of empirical concept we might mistakenly want to define in an empirical science. I grant that ‘sublimed quicksilver and sulphur give cinnabar’ (the ‘technical concept’) is not itself a definition. But the success of this synthesis procedure reveals the elemental composition of cinnabar. And there is no doubt that Kant is using the term ‘definition’ in its technical sense. The passage continues: ‘*Definitio nec sit latior nec sit angustior* [the definition is neither broader nor narrower]’. This is Kant’s gloss on definitions proper (24:265-7; 24:759; 24:924-5).

³⁰ Kant’s view, as I reconstruct it, bears striking similarities to much recent work in philosophy of chemistry. Many have observed that the chemist ‘know[s] through making’ (Bensaude-Vincent 2009, 167), and that ‘making something’, not refutation, ‘is the leitmotif’ of chemical investigation (Hoffmann 2007, 321).
significance of the distinction between given and made *a posteriori* concepts. The distinction lies, I believe, behind Kant’s famous words in the B-Preface to the *Critique* (Bxii-xiii, my emphasis):

> When ... Stahl changed metals into calx and then changed the latter back into metal by first removing something and then putting it back again, a light dawned on all those who study nature. They comprehended that *reason has insight only* into what it itself produces according to its own design ... .

Made *a posteriori* concepts are not, on my reading, simply gleaned from experience. Like mathematical concepts, made *a posteriori* concepts constitute a cognitive achievement.
5 References


Boerhaave, Herman. 1735. Elements of chemistry. Translated by Timothy Dallowe. London, UK: Printed for Pemberton et al.


Oberst, Michael. n.d. "Kant on real essence as the formal nature of a thing.” Cited with permission.


6 Appendix: original German passages


Refl. 2394: Wir sehen nichts ein, als was wir machen können.

Refl. 2398: Wir begreifen‘ nur, was wir selbst machen können.

(‘Begreifen’ is to have insight that ‘is sufficient for a certain purpose’ (24:133)).

Refl. 2402: Die methode der inversion ist die, da ich aus den Erklärungsgründen umgekehrt den Begrif des Erklärten wieder a priori hervorbringen kan. e. g. Chemie, welche mineralische wasser auflöset uns sie wieder hervorbringt, nicht aber Wein. ... Ob ich einen zergliederten Begrif synthetisch wieder hervorbringen kan, muß sich aus den Eigenschaften, die daraus fliesen, zeigen.

Refl. 2930: Der Mathematicus in seiner Definition sagt: sic volo, sic iubeo.


Refl. 5221: Wir müssen uns, wenn wir die Erscheinung vollstandig apprehendirten, einen Erzeugungsbegrif‘ machen können. Dieser ist aber nur möglich, wenn das zufällige, was geschieht, im ganzen genommen oder in seiner ganzen Bestimmung genommen notwendig ist.

(‘Made concepts are ‘von uns erzeugen’ (24:131; A234=B287; 2:282), hence my translation of ‘Erzeugungsbegrif’.)