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Effects of Internal Resistance on Performance of Batteries for Electric Vehicles

Rohit Anil Ugle
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EFFECTS OF INTERNAL RESISTANCE ON PERFORMANCE OF BATTERIES FOR ELECTRIC VEHICLES

by

Rohit A Ugle

A Thesis Submitted in Partial Fulfillment of the Requirements for the Degree of Master of Science in Engineering at The University of Wisconsin-Milwaukee

August 2013
ABSTRACT

EFFECTS OF INTERNAL RESISTANCE ON PERFORMANCE OF BATTERIES FOR ELECTRIC VEHICLES

by

Rohit A Ugle

The University of Wisconsin-Milwaukee, 2013
Under the Supervision of Professor Anoop K. Dhingra

An ever increasing acceptance of electric vehicles as passenger cars relies on better operation and control of large battery packs. The individual cells in large battery packs do not have identical characteristics and may degrade differently due to their manufacturing variability and other factors. It is beneficial to evaluate the performance gain by replacing certain battery modules/cells during actual driving.

The following are the objectives of our research. We will develop an on-line battery module degradation diagnostic scheme using the intrinsic signals of a battery pack equalization circuit. Therefore, a battery “health map” can be constructed and updated in real time. Next based on the derived battery health map, the performance of the battery pack will be evaluated a user specified trip so as to evaluate the “worthiness of replacing” certain modules/cells.

Different electric vehicles have different performance for the same driving cycle. These variations are due to variation in driving patterns, traffic, different light patterns, random
behavior of the drivers etc. To account for this random behavior of the electric vehicle performance we generate 100 random trip cycles. We aim to model the behavior of the driving cycle and battery behavior.

Finally, the thesis also explores the possibility of energy exchange between the battery packs and the smart grid. In the smart grid scenario where we have the knowledge of the electricity price and the load patterns on the grid, it is beneficial for the user to schedule charging and discharging patterns for electric vehicles. Our research will define charging and discharging patterns throughout the life of the battery. We will optimize the charging and discharging times and define the opportunity cost for each day during summer and winter months. The objective is to maximize the profit earned by selling excess energy in the battery to the grid and minimize the charging cost for the electric vehicle.
Dedicated to my wife Mithila and my Parents who always motivated and supported me to continue my education
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1. Introduction

An ever increasing need for better and efficient transportation has motivated the automobile industry to look for alternative sources of energy in lieu of conventional energy sources. The electric vehicles are clean i.e. they have lower CO₂, CO and hydrocarbon emissions than the conventional energy resources. The vehicles which use non-conventional energy sources are multi sourced vehicles which use petroleum-battery, diesel-battery or fuel cell-battery etc. The battery forms a critical element for driving non-conventional vehicles. Electric vehicles (EV) require large battery packs with high energy and power densities to become a competitive choice of transport. These batteries have many cells/modules in series and parallel. Acceptance of these vehicles results from better operation and control of large battery packs.

Recently, addressing the problems of green house effect, clean energy requirements and the need for renewable energy resources, electric vehicles have gained ground [1]. Today’s research in electric vehicle design and battery technology is a major challenge. The automobile industry is due for a major overhaul to achieve minimum pollution, overcome the problem of limited availability of conventional energy resources, and minimize the cost of travelling [2].

There is a continuous increase in the need of energy around the globe. The sources of energy have been changing drastically in the last decades. We all know that the conventional energy sources such as gasoline, coal etc are finite and there is a need to find alternative energy sources to cater to our energy requirements. Renewable energy
resources have been contributing to the energy requirement. An effort to reduce the cost of renewable energy sources like wind energy and solar energy is the need of the hour.

In Fig. 1.1, it can be observed that the major source of energy for transportation is petroleum i.e. 94% and only 3% comes from renewable energy sources [3]. The major reason for this is the availability of renewable energy sources to drive the vehicles on their own is not practical a option; whatever comes in the 3% is the energy from the grid which is stored in the electric vehicle battery or electric locomotives which are connected to the grid. Hence, to satisfy our energy need we have to depend on the energy from the...
grid and limit the use of internal combustion engine. But, the current electricity has many limitations and there are limitations on the infrastructure support.

It is our primary requirement if we have to move from non-renewable energy resources to renewable energy resources we should have a very robust grid which can support the energy needs. The grid should be able to support the additional loads from the electric vehicles. Also, it should be able to meet the variable energy load which varies depending on the time and the season. The cost of energy should not increase with the increase in energy requirement and the grid should also not fail under additional loads.

The modern grid, which incorporates the provision for advanced loads and providing energy efficient solution is depicted in Fig. 1.2. The modern grid is also known as “smart grid” as it can keep a track on the energy price per hour, source of energy during an hour and it would be a self healing grid which solves problems like voltage fluctuations, black
outs etc. It can fix its own operating fixed voltage and can correctly monitor the high voltage on the grid. The best feature in the grid is that a user can be the customer for energy or can sell the excess energy, i.e. which means that there would be a two way interaction between the user and grid. This will help in monitoring energy levels at peak hours. We will limit our application of the smart grid to electric vehicles and their operation.

1.1 Hybrid and Plug-in Hybrid Electric Vehicles

Vehicles, which consist of two sources of energy in combination for propulsion are termed as the hybrid or plug-in hybrid electric vehicles. The source of energy used for driving the vehicles can be a combination for any of the following: diesel, gasoline, battery, bio-fuels, fuel cells etc. Hybrid-vehicles are recognized in today’s market and are being appreciated for their low operation cost and low exhaust emissions. Hybrid-vehicles with a combination of diesel and battery are less efficient than gasoline and battery combination. Hybrid-vehicles with fuel cell and battery are more efficient than gasoline and battery hybrid-vehicle, but they are commercially less successful because of the flammable properties of hydrogen. Also, hydrogen has storage limitations. Hence, more work is required on this front so as to make hydrogen and battery combination successful. Hybrid and Plug-in hybrid electric vehicles are classified based on their power train configuration

- Parallel hybrid
- Series hybrid
- Power split hybrid
1.1.1 Parallel Hybrid Vehicle

In parallel hybrid vehicles the electric motor and IC engine are coupled together. In these types of hybrids, the energy from the two sources is applied on the same shaft and the speed of the two shafts is equal. The output torque is the sum of torque from the engine and the battery. The electric motor torque is positive when the vehicle is driven and negative when regenerative charging is done during braking.

1.1.2 Series Hybrid Vehicle

This type of architecture is mainly observed in electric vehicles which are manufactured for extended driving range. They are also known as range extended electric vehicles.
(REEV). They are typically battery driven electric vehicles but have an internal combustion engine used while driving long distances. This arrangement is common in diesel electric locomotives and ships. This architecture is also used in Chevrolet Volt.

**Power-Split Hybrid Vehicle**

![Diagram of power-split hybrid vehicle](image)

Fig. 1.5. Architecture of power-split hybrid

The power split hybrid vehicle works on the principle of decoupling of the power supplied by the engine from the power demanded by the driver. The power split hybrid incorporate devices allowing for power paths from the engine to the wheels that can be either mechanical or electrical.

The overall battery health is very critical for performance of the electric vehicles. As they are divided and sub-divided into various modules, the module health becomes crucial factor for the performance of the battery. In this thesis, we will study the performance of each module of the battery during equalization for a specific trip. There is significant power loss during the equalization process due to the increased internal resistance, and such loss is also affected by the driving cycle (or the trip pattern). It is of EV customers’ interest to evaluate the (negative) consequences of degraded module(s) and decide if
replacement is necessary. The decision of replacement thus relies on a combination of both diagnosis of physical conditions and economical payback.

Any electric vehicle user desires to know: 1) how much energy loss would be induced for a specific driving trip based on the knowledge of module characteristics within the battery pack, and 2) for the given battery pack, what energy efficiency will the user achieve by replacing certain degraded module or cell with a healthy one. We can investigate the battery health from the internal resistance of the battery pack.

We also know that with the rise in internal resistance, the battery performance deviates and degrades. This results in a rise in the charging time and degraded performance of the battery pack during the driving cycle. Also, with the charging scenario in the smart grid we have the opportunity to decide the charging times, and supply energy to the grid to decrease the cost of the trip. A prior knowledge of the trip/driving cycle, cost of energy on the grid, the battery internal resistance and the energy requirement of the trip enables us to decide the charging and discharging times.

In this thesis, we propose to quantitatively measure the evaluation of module based replacement, named as the “Worthiness of Replacement” (WOR). For a given driving cycle, the WOR of a specific battery pack is defined as the ratio of the state of charge (SOC) change of the current battery pack to that after replacing certain module with a healthy module of nominal specifications. We will measure the Opportunity Cost (OC) for a given vehicle classified as per their age. The opportunity cost for the vehicles is the ratio of the average cost of charging to the average cost of exchange of energy to the grid.
The remainder of thesis is organized as follows, Chapter 2: Literature review: Presents discussion on various battery models and performance of the batteries during a specific driving trip. We study various equalizing schemes. Also, we study the effect of voltage during the equalization process. Chapter 3: Presents Simulation Results for Equalization: We derive the electric vehicle model. Then we estimate the performance of the batteries during equalization. We calculate the exact amount of energy lost during the process of equalization. Based on the energy loss in the equalization process, we generate a worthiness of replacement (WOR) number. Chapter 4: Presents Simulation Results for analyzing performance of group of batteries Group Performance: In this chapter we assume that we have 4 groups of electric vehicles consisting of 100 vehicles each. These groups are classified based on the age and internal resistance of the batteries. We intend to minimize the cost of the trip by minimizing the charging cost and maximizing the profit earned through exchanging the energy with the grid. We propose opportunity cost for the user for each vehicle. Finally, Chapter 5: we summarize our results and observations from various simulations.
2. Literature Review

In this chapter the electric vehicle model is reviewed. We formulate all the equations which are useful to model an electric vehicle under driving conditions. Also, various types of batteries and battery models are studied with their application. Large battery packs have varied properties and performance under same or different operating conditions. They are subjected to equalization to optimize and improve their performance. We review current controlled as well as voltage controlled equalization schemes.

2.1 Electric Vehicle Model

In order to derive expressions for motor driving torque and motor driving current, we need propulsion dynamics first. Vehicle propulsion dynamics is dependent on aerodynamic force, acceleration force on the vehicle, and rolling resistance force.

2.1.1 Aerodynamic Force

The aerodynamic force is the force due to friction on the moving body from the air. This force takes into consideration the protruding shapes and surfaces, ducts passages, spoilers, frontal area of the vehicle.

\[ F_{ad} = \frac{1}{2} \rho AV^2 \]  \hspace{1cm} (2.1)

where, \( \rho \) is the air density, \( A \) is frontal area, \( C_d \) is the coefficient of drag and \( V \) is the velocity of the vehicle.
A good design can effectively reduce the force due to drag by reducing the frontal area from the shape and also reduce coefficient of drag.

2.1.2 Rolling Resistance

The rolling resistance force is due the contact of tires with the road. This force is independent of the velocity of the vehicle. The type of tire and tire pressure are the major factors contributing to this force.

\[ F_{rr} = \mu_{rr} Mg \]  

(2.2)

where, \( \mu_{rr} \) is the rolling resistance coefficient, \( M \) is the mass of the vehicle and \( g \) is the acceleration due to gravity. Proper pressure in the tires and quality of tires contribute to a smaller resistance force.

2.1.3 Acceleration Force

The acceleration force is responsible for linear acceleration of the vehicle. The acceleration force is given by Newton’s second law of motion as

\[ F_{acc} = Ma \]  

(2.3)

This the actual acceleration applied to the vehicle during its motion. This includes the rotating as well as translating parts in the vehicle.

2.1.4 Wheel Torque

All the forces on the vehicle contribute to the torque at wheels which propels the vehicle. The torque at the wheels from these driving forces is
\[ T_{wh} = (F_{ad} + F_{rr} + F_{acc})r \]  \hspace{1cm} (2.4)

where, \( F_{ad} \) is the aerodynamic force, \( F_{rr} \) is the rolling resistance force, \( F_{acc} \) is the accelerating force, and \( r \) is the radius wheel.

### 2.1.5 Motor Torque

In case of electric vehicles the output torque requirement is satisfied by the electric motor. To complete specified motion of the wheel electric motor produces torque at the motor shaft. The torque at the motor shaft is

\[ T_m = \frac{T_{wh}}{G \cdot \eta_g} \]  \hspace{1cm} (2.5)

where, \( T_{wh} \) is the torque at the wheels, \( T_m \) is the torque at the motor, \( G \) is the gear ratio and \( \eta_g \) is the gear efficiency.

### 2.2 Electric Motor Model

Modeling electric motor to satisfy the required motion of the vehicle is the primary requirement of the electric vehicle. The propulsion of the electric vehicle is completely dependent on the electric motor. The factors which are considered for electric vehicles are acceleration requirement, speed requirements, life of the motor and regeneration requirements. Also, there are limiting factors for modeling the performance of the motors which are motor torque requirement, angular speed and acceleration. The performance of the motor helps to increase the tire life. It also keeps a check on the maximum speed the vehicle can be driven. If these design requirements are not considered, the performance of the electric vehicle is adversely affected.
We have the design requirements and the expected performance from the electric motor. The parameters to design the electric motor are resistance (Ω), motor inductance (L), back emf constant (volt-sec/rad), torque constant (N-m/a), rotor inertia (kg*m²) and mechanical damping. The automotive parameters considered are vehicle damping (friction), transmission dynamics, gear ratio and tire friction on the pavement. The electric motor is scaled based on motor speed and torque range. We have limit on the torque and speed of the motor. Also, to safeguard motor from burning out, we set a limit for maximum current and voltage. Efficiency of the motor varies with motor torque, power and motor size. Thus interpolating efficiency with the motor torque and speed is used calculate input and output power of the motor at wheels.

The input power required by the motor from the battery is

\[ P_i = \frac{P_0}{\eta_0} \]  \hspace{1cm} (2.6)

where, \( P_i \) is the input power and \( \eta_0 \) is the motor efficiency

\[ P_0 = \frac{P_W}{\eta} \]  \hspace{1cm} (2.7)

where, \( P_0 \) is the output power, \( P_W \) is the power required at wheels and \( \eta \) is the gear efficiency

The type of electric motor selected for electric vehicle is dependent on the type of motor used. AC motors have robust performance, but they fail to react to sudden changes in speed; DC motors perform ideally under sudden acceleration and deceleration. Therefore
the choice of motor is a tradeoff between performance during acceleration and running under high speeds. Following are some of the typical configurations of permanent magnet synchronous motors used for electric racing cars.

Table 2.1. Typical permanent magnet electric motor configurations

<table>
<thead>
<tr>
<th>Motor Name</th>
<th>YASA-400</th>
<th>YASA-750</th>
<th>YASA-750H</th>
</tr>
</thead>
<tbody>
<tr>
<td>Peak torque 400A</td>
<td>400Nm</td>
<td>750Nm</td>
<td>750Nm</td>
</tr>
<tr>
<td>Continuous torque</td>
<td>220Nm</td>
<td>400Nm</td>
<td>400Nm</td>
</tr>
<tr>
<td>Peak power ~ 400V</td>
<td>100kW</td>
<td>100kW</td>
<td>150kW</td>
</tr>
<tr>
<td>Continuous power</td>
<td>85kW</td>
<td>50kW</td>
<td>70kW</td>
</tr>
<tr>
<td>Peak efficiency</td>
<td>95%</td>
<td>95%</td>
<td>95%</td>
</tr>
</tbody>
</table>

Yasa motors is a leading manufacturer of electric motor drives. They specialize in high power and high torque density electric motors to market. The Yasa motors in Table 2.1 are permanent magnet synchronous motors that can be used in hybrid electric vehicles and pure electric vehicles. These motors have varied applications from industrial settings to run motors for electric cars.

### 2.3 Electric Vehicle Battery

Electric vehicle battery consists of long series and parallel connected batteries. Batteries convert chemical energy into electrical energy. Direct current (DC) is generated in the batteries from the positive and negative electrodes in the electrolyte. The cells which convert chemical energy to electricity only once in their life are called primary cells where as the rechargeable cells are called secondary or rechargeable batteries. The
rechargeable batteries can be charged by reversing the chemical reactions in the battery. Thereby bringing the batteries to their original state of charge. The batteries used for electric vehicles are rechargeable batteries which propel the electric motor. Electric vehicle batteries undergo deep discharge so as to satisfy the need of power. Hence the electric vehicle batteries should have high ampere-hour (Ah) capacity. The following are the characteristics the electric vehicle must have:

- High energy density
- High calendar life
- Low cost batteries
- Low replacement cost
- High reliability
- Robustness
- Low weight and smaller sizes
- Higher power to weight ratio

The major drawback for electric and plug-in hybrid electric vehicles is their range of travel. Vehicle with internal combustion engine (ICE) have no limiting range for travel whereas electric vehicles have maximum of 30-350 miles all electric range. Electric vehicles have lower specific energy which results in poor performance during initial acceleration compared to internal combustion engines. This means that the electric vehicles have lower initial acceleration as the batteries are restricted from performing
sudden deep discharging cycles which degrade the battery life, and also the motor responds slowly to changes in acceleration. On the other hand, the internal combustion engines can provide power efficiently starting the vehicle from rest without degrading the life of engine. The types of batteries commercially available are given below.

Table 2.2. Commercially available batteries

<table>
<thead>
<tr>
<th>Battery</th>
<th>Specific Energy (Wh/Kg)</th>
<th>Energy Density (Wh/L)</th>
<th>Specific Power (W/Kg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lead Acid</td>
<td>30-40</td>
<td>60-70</td>
<td>180</td>
</tr>
<tr>
<td>NiCad</td>
<td>40-60</td>
<td>50-150</td>
<td>150</td>
</tr>
<tr>
<td>NiMH</td>
<td>60-120</td>
<td>140-300</td>
<td>250-1000</td>
</tr>
<tr>
<td>Li-Ion</td>
<td>100-265</td>
<td>250-730</td>
<td>250-340</td>
</tr>
<tr>
<td>Zinc-Air</td>
<td>470</td>
<td>270</td>
<td>100</td>
</tr>
</tbody>
</table>

The two main commercially available batteries are lead acid and lithium Ion batteries. Currently, there is extensive research conducted for using Nickel metal hydride batteries and Zinc Air batteries for driving commercially available electric vehicles. The batteries are also used with fuel cells but there is no commercial application of fuel cell and battery hybrids.
The batteries which are widely used are compared in Table 2.3.

Table 2.3. Comparison for Lithium Ion and lead acid batteries

<table>
<thead>
<tr>
<th>Property</th>
<th>Lithium Ion</th>
<th>Lead Acid</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal cell voltage</td>
<td>3.5 V</td>
<td>2 V</td>
</tr>
<tr>
<td>Amp-hour efficiency</td>
<td>~90-95%</td>
<td>~80%</td>
</tr>
<tr>
<td>Internal resistance</td>
<td>Very low</td>
<td>Extremely low</td>
</tr>
<tr>
<td>Operating temperature</td>
<td>Ambient</td>
<td>Ambient</td>
</tr>
<tr>
<td>Self-discharge</td>
<td>~10% per month</td>
<td>~2% every day</td>
</tr>
<tr>
<td>Number of life cycles</td>
<td>greater than 1000</td>
<td>Up to 800</td>
</tr>
<tr>
<td>Recharge time</td>
<td>2-3h</td>
<td>8h</td>
</tr>
</tbody>
</table>

2.3.1 Lithium Ion Batteries

The lithium ion battery is a member of the rechargeable battery family. In lithium ion batteries, the lithium ion moves from negative electrode to positive electrode during discharging and arrives at positive electrode while discharging. The three primary components of the lithium ion batteries are the positive electrode, negative electrode and electrolyte. The negative electrode is made from carbon, positive electrode is a lithium metal oxide and the electrolytic solution is the lithium salt in an organic solvent. The
direction of the lithium ions change between anode and cathode based on the direction of the current flow.

A typical lithium ion battery pack during its early formations is as shown in Fig. 2.1. Lithium batteries first came into existence in 1970 by M.S. Whittingham, while he worked for Exxon [4]. The major drawback with the lithium ion batteries is that lithium is highly explosive and there are safety issues working with lithium ion batteries. The present form of lithium ion batteries came into existence in 1985, by Akira Yoshino [5]. He assembled lithium ion electrodes, lithium cobalt oxide and carbonaceous electrolyte. The performance of lithium ion batteries are best suited for applications like electric vehicle as the batteries are light weight and have high energy density.

**2.3.2 Battery Modeling Technique**
So as to model a particular type and application of the battery with R-C circuits, we must know the behavior of the battery. The performance of the battery is dependent on 30-40 variables. The model of battery generated is strictly for that specific battery. The models of batteries are used to understand the performance of the battery and its behavior which requires the knowledge of fundamental physics and chemistry. Parameters like temperature, voltage, resistance and current can be measured with greater accuracy. Based on these parameters we can model the performance of electric vehicle batteries using lesser complicated R-C circuits. The battery models generate accurate state of charge (SOC) and open circuit voltage (VOC) of the battery. If the battery SOC or VOC fall below a certain limit, their characteristics change permanently, this degrades their performance. The charging and discharging resistance of the batteries is of critical importance as it the performance determining factor. It can be calculated based on the type of the battery [6]. Electric vehicle battery model must account for self discharging resistance and the operating temperature of the vehicle.

The model we consider for our research does not include self discharge resistance as we do not simulate over long term behavior of the model, in which case this resistance would be meaningful. Also, we do not account for the effect of temperature on the battery performance as we assume that the operating range of the temperature is very small i.e. the operating range of the electric vehicle battery is small.

2.3.3 Battery Equivalent Circuit Representation

The crucial parts for electric vehicles are low power dissipation and maximum battery run time. An accurate circuit model can solve the problem of predicting and optimizing battery run time and circuit performance. The dynamic model must account for all
dynamic characteristics of the non-linear open circuit voltage, current, temperature, cycle number and storage time dependent capacity to transient response.

Fig. 2.2. Battery model examples (a) Thevenin electrical model

(b) Impedance based electrical model

We can observe in Fig. 2.2(a) the most basic form of battery equivalent R-C model connections is shown. The battery consists of a series resistance and a parallel R-C connection to predict the open circuit voltage and SOC of the battery [7,8]. The major
The drawback of the battery is that it assumes open circuit voltage as constant and this assumption makes it impossible to predict steady state battery variation [9]. The electrochemical impedance spectroscopy in Fig. 2.2(b) obtain an AC equivalent impedance model in the frequency domain and then use a complicated equivalent network ($Z_{ac}$) to fit the impedance spectra. The drawback for this method is that it’s difficult, complex and non-intuitive. Also, they only work for fixed SOC and temperature setting [10].

![Fig. 2.3. Runtime Based Electrical Battery Models](image)

The Runtime based battery model is as shown in Fig. 2.3 use a complex circuit network and a DC voltage [11]. They cannot predict voltage response with varying loads and runtime voltage [12].

In 2007, Vasebi et al developed an extended kalman filter for estimating the SOC which was a nonlinear estimating technique for accurate prediction performance of the SOC.
As shown in Fig. 2.4, $V_t$ is the terminal voltage or open circuit voltage, $R_t$, $R_s$ and $R_e$ are terminal resistance, surface resistance and bulk resistance respectively, $C_s$ and $C_b$ are surface capacitor and bulk capacitor respectively. In this battery model the SOC is predicted from the voltage on the bulk capacitor. The value of the bulk capacitor is constant. This type of RC model can be used for lithium ion as well lead acid batteries in conjunction with extended kalman filters [13].

With extended kalman filters, even though the accuracy for measuring SOC increases but problems like SOC drift due to overcharging or ambient temperature fluctuations still persisted. In 2009, to address this issue, Gould C.R. et al proposed a remapped RC model to perform improved modeling capacities and accurately estimate the dynamic model parameters.
In Fig. 2.5, $R_p$ is the self discharge resistance which is very large compared to the overall resistance of the battery. $C_n$ and $R_n$ are capacitor and resistor in series in the model. The change in $C_p$ over a considerable period of time will be the representation of the state of health (SoH) for the battery. $R_i$ is the resistance of the battery terminals and inter-cell connections. $C_p$ and $R_p$ are capacitor and resistors in parallel.

### 2.3.4 Battery Equalization

A serious problem which affects battery performance is the voltage across each battery. Electric vehicle consists of more than 80-100 cells in each battery. The cells have varying internal properties which results in variation in the open circuit voltage. Since SOC is based on the open circuit voltage, if there are errors present in the open circuit voltage measurement, there will be errors in SOC measurements. Also, the battery performance is degraded if wrong measurements for SOC are considered for the battery. To avoid
uneven performance of large group of batteries, they are forced to exhaust energy in the heat sink. This results in loss of energy and increases the cost of travelling and utilizing batteries.

To address the problem of variation of voltage in series connected cells for electric vehicles, many techniques have been developed [14]. To make the equalization process implementable, cost effective and to keep the voltage and current stresses low, modular charge equalization process was developed by H. Park et al. In this technique, the battery pack is divided in many small modules and then intra-module equalizer and outer module equalizer are designed [15].

Fig. 2.6. Multi-winding transformer (a) Conventional Approach (b) Modularized Approach

A battery pack with series connected cells is shown in Fig. 2.6(a). The same battery pack with modularized design pattern is shown in Fig. 2.6(b). The battery pack is divided into
maximum number of 8-10 cells per module, many modules in series form a battery pack. With the formation of modules we overcome problem of mismatched inductance leakage and implementation of the modules becomes easier.

2.4 Smart Grid

The success of implementing hybrids into the market largely depends on the infrastructure of charging the vehicles from the grid [16]. To build a strong grid network, renewable energy sources like wind energy, solar energy, batteries etc are used along with the conventional sources of energy. Continuous effort is made to lower the cost of energy generation to support the grid [17]. This has led to novel concepts of smart grid where there could be energy exchange from the grid to the end user and from the end user to the grid [18,19]. Not only we can predict the load and price of the energy for the next day, but we can identify the source of power during a specific time of the day. This concept could be very beneficial for setting up the charging algorithms for electric vehicles [20,21]. The concept of smart grid has motivated researchers to optimize the cost of operation of the grid and its maintenance. The cost of producing and supplying electricity from various sources is minimized using the available renewable and non-renewable sources of energy and the nature of load which is applied on the grid. The load on the grid is time dependent, so does the cost of energy which varies with time, season and many other factors [22]. It is widely known that the load on the grid is lowest during nights which bring the prices of the electricity to its lowest, whereas the load during the day time is the highest, which forces the prices to its maximum values [23].
Increasing the number of electric vehicles in the market will compel the grid to support the additional load. The charging time for electric vehicles is mostly during the nights. The grids have lower loads during nights as compared during the day. Also, the price of electricity during the night is lowest which helps to minimize the charging cost [24]. Hence, the grid load and electricity price could be regulated.

Electric and plug-in hybrid vehicles use large battery packs, containing batteries in series and parallel arrangement to obtain required battery configuration. Electric vehicles can now-a-days travel more than 100 miles with one complete charging cycle which is significantly more than daily commuting distance from home to office and back home. This allows us to look at the electric vehicles as the potential supplier of energy to the grid. These batteries have independent cell/module properties because of their manufacturing process and variability in the processes they undergo [25]. Also, they degrade and respond independently to different conditions to which they are exposed. Batteries deteriorate with age and their performance drops down significantly [26]. The knowledge of the trip to be travelled, the age of the battery and the time required for charging will help us identify the amount of energy available with any vehicle selected at random. This helps to determine the amount of energy that is available from the batteries that can be exchanged with the grid.
3. Simulation Results for Equalization

In this chapter we discuss electric vehicle under various driving conditions. We model the battery which is exposed to equalization process during the driving cycle. We calculate the loss for battery for two module equalization process and then with three module battery. We calculate the “Worthiness of Replacement” (WOR) for two module and three module case. We also estimate the loss in the batteries with higher internal resistance. We can quantify the loss in the process of equalization.

3.1 Electric Vehicle and Motor

D.C. motors have limitations on life and they are not robust as to A.C. motors. The A.C. motors have a sluggish response, whereas D.C. motors have faster response. These drawbacks are overcome by permanent magnet synchronous motor (PMSM). The PMSM motors are robust and their performance for initial acceleration is better than the A.C. motors. The motor we use for our research is permanent magnet synchronous motor with a gear box transmission. The motor is a 4-pole 560V synchronous motor with rated speed of ~5000rpm. The torque limits were ~140N-m and ~160N-m during driving and braking respectively. The following are the electric vehicle parameters used by us in our simulation study:
Table 3.1. Configuration of electric vehicle.

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Mass ($M$)</td>
<td>1560 kg</td>
</tr>
<tr>
<td>Gear Ratio ($G$)</td>
<td>11</td>
</tr>
<tr>
<td>Coefficient of Drag ($C_d$)</td>
<td>0.19</td>
</tr>
<tr>
<td>Coefficient of Rolling Resistance ($\mu_{rr}$)</td>
<td>0.0048</td>
</tr>
<tr>
<td>Gear Efficiency ($\eta_g$)</td>
<td>0.95</td>
</tr>
<tr>
<td>Radius of the Wheel ($r$)</td>
<td>0.3 m</td>
</tr>
</tbody>
</table>

3.2 Battery Equivalent Circuit

Simulating a practical driving situation demands modeling of the parts required for driving the electric vehicle. The major part of the electric vehicle simulation is the battery model and parameters of the battery. The battery model will predict the performance of a real life battery under actual driving condition. We have the access to open circuit voltage, current, internal resistance and SOC remaining on the battery pack. This gives the driver an idea of electric range of the battery.
In Fig. 3.1 R-C model of the battery is given where $C_S$ and $C_L$ are surface capacitance and bulk capacitance, respectively. $R_S$, $R_L$ and $R_0$ are surface resistance, bulk resistance and series resistance, respectively. In general, $R_0$ and $R_S$ are much smaller than bulk resistance $R_L$. Similarly, surface capacitance $C_S$ is much smaller than bulk capacitor $C_L$.

### 3.3 Battery State of Charge Calibration

Knowledge of the state of charge of a battery in a real-time traffic situation is very important. It is this capacity that determines the range an electrical vehicle can travel. State of charge is also called the “fuel gauge” since it serves a function similar to a fuel gauge in a conventional car. SOC is defined in percentages and the techniques to determine the capacity is very crucial, as battery performances are unpredictable to a large extent and is dependent on many parameters.

SOC is defined as the ratio of the electric charge $Q(t)$ which can be delivered by the battery at any instance of time to the nominal capacity of the battery $Q_o$. Mathematically,
the state of charge is given as below

\[ SOC(t) = \frac{Q(t)}{Q_0} \]  

(3.1)

The charge remaining on the battery varies with time and various environmental factors. Also, the ageing of the battery should be taken into consideration. The following are different SOC measurement techniques:

1. Direct Measurement technique
2. SOC from the specific gravity measurements
3. Internal Impedance of the battery
4. Coulomb counting (Current measurement)
5. SOC based on the open circuit voltage

The deterministic techniques mentioned above can estimate the SOC accurately based on the application. The most efficient and accurate techniques for estimating SOC for electric vehicles are based on open circuit voltage and coulomb counting. Coulomb counting can be used for estimating SOC for a short period of time like during a day or over a span of few months [27]. Open circuit voltage of the battery is an accurate measure for the health of the battery, so the variation of the SOC with the age of the battery is accounted in the open circuit voltage. Thus, we use SOC measurement based on open circuit voltage throughout the life of the battery.

We drive our electric vehicle for a specific driving trip. We do not consider the change in battery of the electric vehicle throughout its life. We can efficiently consider coulomb
counting method for estimating the SOC for the vehicle we simulate. We have assumed the current leaving the battery as positive current, i.e when the electric vehicle is driven by the battery. We also assume the current entering the vehicle is negative, i.e the current when the motor acts as the generator and the battery is charged. The SOC is then calculated depending on the current transfer from the battery every second. SOC for an electric vehicle under driving condition is given by

$$SOC(k+1) = SOC(k) - \frac{V_{oc} - \sqrt{V_{oc}^2 - 4(R_{int} + R_t) \cdot T_m \cdot \omega_m \cdot \eta_m \cdot \text{sgn}(T_m)}}{2(R_{int} + R_t) \cdot Q_b}$$

(3.2)

where,

- $V_{oc}$ = Total open circuit Voltage of the battery (Volts)
- $T_m$ = Electric motor torque (N.m)
- $\omega_m$ = Electric motor speed (rad/sec)
- $\eta_m$ = Electric motor efficiency
- $R_{int}$ = Internal impedance of the battery (ohms)
- $R_t$ = Terminal impedance (ohms)
- $Q_b$ = Battery capacity (Ah)

SOC (k) is the state of charge at the k-th step
3.4 Battery Equalization Scheme

As the voltage in a single cell is quite low, for high voltage applications like EV, battery modules and packs are made via serial and parallel combinations of the cells [28]. Variations are inevitable in the internal resistances of the battery cells and modules. The variation in the internal resistance is caused by extrinsic or intrinsic cell properties, contact resistance among cells, or temperature gradient because of improper thermal management accounts for battery imbalance. The variation in the internal resistance causes variations in the SOC and degrades the cell [29]. The battery life can be significantly affected by the imbalance among modules or cells due to the associated over-charging or over-discharging. Hence, equalizing the modules or cells is important for acquiring the maximum achievable power and extending the battery life [30,31].
In this study, the voltage equalization scheme by Lee and Cheng is adopted [32] with a two-module situation shown in Fig. 3.2. The voltage of each module determines the direction of energy transfer between the two modules with proper operation of the MOSFET switches $Q_1$ and $Q_2$. $L_1$ and $L_2$ are two uncoupled inductors, while $C_0$ is an energy transferring capacitor. $V_{B1}$ and $V_{B2}$ are battery voltages for modules (or cells) 1 and 2, respectively. For normal condition, $V_{C1} = V_{B1} + V_{B2}$. The ideal condition is $V_{B1} = V_{B2}$, although this can seldom be the case in realistic operation. The operational scenario for a PWM is shown below.
Fig. 3.3. Typical switching waveform of the battery equalizer when $V_{B1} > V_{B2}$.

1) $V_{B1} > V_{B2}$: For duration $D_{TS}$, $Q_1$ is turned on, and capacitor $C_1$ transfers energy to $V_{B2}$ during the same period inductor $L_1$ stores energy. For duration $(1-D_{TS})$, $Q_1$ is turned off, $D_2$ turns on, and the capacitor energy is supplied to Module#1 and $L_2$ charged by $V_{B2}$. In the switching duty cycle ($T_s$), as shown in Fig. 3.3, $T_1 - T_0 = D_{TS}$, while $T_2 - T_1 = (1-D_{TS})$. The operation can be described by the following equations.
a) For $t \in [T_0, T_1]$, $Q_1$ is turned on, which implies

$$V_{B_1}(t) = L_1 \frac{d i_{L_1}(t)}{dt} \quad i_{L_1}(T_0) = I_0$$

(3.3)

$$V_{B_2}(t) = -L_2 \frac{d i_{L_2}(t)}{dt} + \frac{1}{C_0} \int_{T_0}^{t} i_{L_2}(\tau)d\tau \quad i_{L_2}(T_0) = I_0$$

(3.4)

b) For $t \in [T_1, T_2]$, $Q_1$ is turned off and $Q_2$ is turned on, which implies

$$V_{B_1}(t) = L_1 \frac{d i_{L_2}(t)}{dt} + \frac{1}{C_0} \int_{T_1}^{T_2} i_{L_1}(\tau)d\tau$$

$$i_{L_1}(T_1) = I_p$$

(3.5)

$$V_{B_2}(t) = -L_2 \frac{d i_{L_2}(t)}{dt}$$

$$i_{L_2}(T_2) = I_p$$

(3.6)

Equations (9) through (13) describe the voltages $V_{B_1}$ and $V_{B_2}$ dynamics during one duty cycle of PWM operation. $I_p$ is the peak current during the operation cycle $D_{Ts}$. The currents in the inductor $I_{L_1}$ and $I_{L_2}$ are given by

$$I_{L_1} = \left[ \frac{1}{2} \left( \frac{V_{B_1}}{L_1} D^2 + \frac{V_{c_1} - V_{B_1}}{L_1} (1 - D)^2 \right) \right] T_s$$

(3.7)

$$I_{L_2} = \left[ \frac{1}{2} \left( \frac{V_{c_1} - V_{B_2}}{L_2} (1 - D)^2 + \frac{V_{B_2}}{L_2} (1 - D)^2 \right) \right] T_s$$

(3.8)

By varying the switching frequency, the equalization scheme can be implemented in continuous current or discontinuous inductor current mode. During the equalization
process, the weak cell is charged by a strong cell to balance the energy level of both the cells. In our study battery 1 is at higher energy level than battery 2.

2) $V_{B1} < V_{B2}$: The operation is controlled by the switching $Q_2$ and $D_1$ in similar fashion as case 1, and similar equations would apply.
3.5 Worthiness of Replacement

The concept of worthiness of replacement (WOR) is applied to the battery pack after the battery is equalized and the trip is complete. As mentioned earlier, though equalization is unavoidable, but WOR projects the exact loss of energy in the trip. This analysis would be the decision making factor for projection of completion of the trip as the onboard energy is calculated. The WOR is defined as

\[
WOR = \left[ \frac{SOC \ Change \ of \ Current \ Battery \ Pack}{Battery \ Pack \ SOC \ Change \ with \ Certain \ Module(s) \ Replaced} \right]
\]  

(3.9)

Equation 3.7 and 3.8 can be enhanced by some averaging operation, for example for actual or predicted trips of certain number of days. The traffic is stochastic in nature as driving behavior such averaging will be helpful to obtain more reliable result for evaluation purpose.
3.6 Driving Cycle

We require motor speed and motor torque to study the simulation behavior of the battery. We start the trip at 124 West Freistadt Road in Thiensville, while the destination is 3200 North Cramer Street in Milwaukee. This is a representative of an ideal driving cycle which consists of highways, street roads, stop and signs and traffic lights, so we have decided to use this driving cycle for our simulations.

Fig. 3.4. Route map of the sample trip

The time for driving trip was ~1614sec. The maximum torque during driving is ~140Nm while the maximum torque during braking or negative torque is ~160N.m. The trip includes constant driving speed cycles, constant acceleration cycles and constant deceleration cycles. This trip includes driving in the city roads, on the freeways. It also
includes stops at the lights. The following driving speed and torque is used as input to the electric vehicle. The current limits on the battery side were set from 250A to -250A.

Fig. 3.5. (a) Motor speed during driving, (b) Motor torque profile during driving
3.7 Two Module Battery Pack

Two battery modules are assumed serially connected. For each module, the capacity rating is 20Ah, respectively. The upper and lower limits of battery SOC are set to be 80% and 30%, respectively. Each module consists of 4 sub-modules which have 7 cells in series, i.e. 28 cells in total, with nominal voltage 3.6V [33]. The voltage across the battery pack is 201.6V [34], i.e. 100.8 V for each module. The internal resistance values used in this research are approximately equivalent to the internal resistance values of the lithium ion batteries from Toyota Prius model. Two cases are simulated with the settings described below (also summarized in Table 3.2, with B-1 and B-2 representing battery modules 1 and 2, respectively):

Table 3.2. Initial Conditions of Two Module Simulation Study

<table>
<thead>
<tr>
<th>Case No.</th>
<th>Battery No.</th>
<th>Voltage(V)</th>
<th>Capacity (Ah)</th>
<th>SOC(%)</th>
<th>Internal Resistance (Ω)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>B-1</td>
<td>100.8</td>
<td>20</td>
<td>80</td>
<td>0.075</td>
</tr>
<tr>
<td></td>
<td>B-2</td>
<td>100.8</td>
<td>20</td>
<td>80</td>
<td>0.075</td>
</tr>
<tr>
<td>2</td>
<td>B-1</td>
<td>100.8</td>
<td>20</td>
<td>80</td>
<td>0.075</td>
</tr>
<tr>
<td></td>
<td>B-2</td>
<td>100.8</td>
<td>20</td>
<td>65</td>
<td>0.30</td>
</tr>
</tbody>
</table>
Case-1: Both modules are in the nominal condition, i.e. having internal resistance of 0.075Ω. Starting from 80% SOC, both modules follow the same discharging trajectory as shown in Fig. 3.6. The final SOC is 53.52%.

![Graph](image.png)

Fig. 3.6. Battery module SOC trajectories for with Case #1 with the example driving cycle

Both batteries have the same internal resistance which is 0.075Ω. The batteries are connected in series which resemble 2 modules. The batteries start discharging at 80% SOC at the beginning of the trip and end at 53.52% SOC at the end of the trip. The electric vehicles travels ~27.5 kilometers in 1614 sec. The battery of the vehicle consumes 26.48% SOC to complete the trip.
Case 2:

Battery-1 is in nominal condition, while Battery 2 is degraded with internal resistance of ~0.30Ω [13]. As battery 2 is degraded, we assume the starting SOC level is 65%. Such difference in SOC level results in the equalization process described earlier.

We observe that the two modules equalize during the first ~645 seconds of the driving cycles. The energy from B-1 charges B-2 to increase its SOC level.

![Diagram showing the SOC levels of Battery 1 (B1) and Battery 2 (B2) over time.](image)

Fig. 3.7. Two Module Battery SOC for example driving cycle for Case-2

The two modules are equalized to 61.8% SOC, and then both modules discharged in identical fashion down to 33.45% SOC by the end of the driving cycle. Though the
driving cycle is complete in case-2, there is a considerable amount of energy loss from B-1 supplied to B-2 so as to equalize which could have been used for driving.

For case-2 in particular, it can be observed in Fig. 3.7 that, due to the relatively large internal resistance of B-2, there is significant amount of energy loss during the equalization from B-1 to B-2. The battery-pack SOC changes by 26.48% in case-1 (both modules healthy), while it changes by 39.05% in case-2. Such difference leads to the WOR of 1.47 for B-2.
3.8 Three-Module Battery Pack

Simulation is then performed for a battery pack with three modules in series. The capacity for each module is ~20Ah. The battery pack is composed of three modules. Each module consists of two serially connected sub-modules of nine cells each, i.e. 18 cells in series. This configuration results is 64.8V across each module. The overall voltage across the battery pack is 194.4V. The internal resistance for ideal module is assumed to be 0.054Ω.

Table 3.3. Initial conditions of individual battery modules for simulation study

<table>
<thead>
<tr>
<th>Case No.</th>
<th>Battery No.</th>
<th>Voltage(V)</th>
<th>Capacity(Ah)</th>
<th>SOC(%)</th>
<th>Internal Resistance (Ω)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>B-1</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>B-2</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>B3</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.054</td>
</tr>
<tr>
<td>2</td>
<td>B-1</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>B-2</td>
<td>64.8</td>
<td>20</td>
<td>72.5</td>
<td>0.081</td>
</tr>
<tr>
<td></td>
<td>B-3</td>
<td>64.8</td>
<td>20</td>
<td>65</td>
<td>0.108</td>
</tr>
<tr>
<td>3</td>
<td>B-1</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.054</td>
</tr>
<tr>
<td></td>
<td>B-2</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.081</td>
</tr>
<tr>
<td></td>
<td>B-3</td>
<td>64.8</td>
<td>20</td>
<td>80</td>
<td>0.108</td>
</tr>
</tbody>
</table>
Three cases are simulated with settings listed in Table 3.3, with B-1, B-2 and B-3 denoting battery modules 1, 2 and 3, respectively.

**Case 1:**

The batteries have state of charge (SOC) mentioned in Table 3.3.

![SOC trajectory for case 1 of three-module battery pack](image)

**Fig. 3.8. SOC trajectory for case 1 of three-module battery pack**

All the modules are in nominal condition, i.e. with internal resistance of 0.054Ω and 80% initial SOC. All batteries are identical and do not vary in their performance for the whole driving cycle. All the modules demonstrate identical discharging trajectories as shown in Fig. 3.8, with the final SOC of 50.84%.
Case 2:

B-1 is in nominal condition, B-2 has internal resistance of 0.081Ω with 72.5% initial SOC, and B-3 has internal resistance of 0.108Ω with 65% initial SOC. This case is intended to simulate B-2 and B-3 as more degraded modules.

Fig. 3.9. Battery SOC trajectories for three modules for Case 2 of Table 3.3

The driving cycle can be completed with the onboard battery power, there is a considerable amount of SOC from B-1 supplied to B-2, and that from B-2 supplied to B-3. Furthermore, due to the relatively higher internal resistances of B-2 and B-3, there is significant amount of energy loss during the aforementioned equalization processes. This
process results in equalization among the three modules from the start till 1005 seconds, as shown in Fig. 3.9. In particular, B-1 has higher SOC than B-2 and B-2 has higher SOC than B-3. The equalization of these three battery modules follow the same logic as described earlier, i.e. the equalization decision is made for every pair of neighboring modules based on the comparison of the relevant voltages, which is done by triggering the associated switches. In the scenario assumed for Case 2, current is discharged from B-1 to B-2, and current is discharged from B-2 into B-3. All the modules equalize their SOC to 45.57%. Afterwards, the three modules jointly discharge to 35.34% SOC by the end of the driving cycle. To complete the same trip, the average SOC drops by 29.16% in Case-1, while in Case-2, by 37.16%. The corresponding WOR is 1.27.

Case 3:

Case-3 involves an analysis to case 2 except that the starting SOC for all the modules is identically at 80%. Simulation has also been performed to the situation when battery module equalization occurs not from the start of the trip, but rather in the middle of the trip as the SOC difference increases. For this purpose, we consider the same battery configuration as in Table 3.3 while all the modules have equal starting SOC, i.e. 80%. The SOC deviates for each module during the first 645 seconds, and then after the equalization process starts. At that point, the SOC difference between Battery-1 and Battery-2 was 2.05% and that between Battery-2 and Battery 3 was 1.53%, respectively. With the equalization process, the modules are equalized to 50.45% by 1050 seconds. Then the whole battery pack completes the driving cycle at SOC 41.95%.
Fig. 3.10. Battery SOC trajectories for three modules for Case 2 for intermediate equalization

The total energy required to travel the trip was 38.05%, and the WOR for the trip was 1.30 in this case as shown in Fig. 3.10.

The above simulation results show that equalization can handle the presence of degraded module during vehicle’s operation however there is a considerable amount of SOC loss during equalization. Highly degraded modules have significantly high internal resistance,
which would waste the battery energy and in turn lead to uneconomical operation. If the module-specific internal resistance can be identified online, the vehicle owners can perform the economical analysis based on their preferred trips, and make reasonable decision on module replacement.
4. Simulation Results for Group Performance

In this chapter, we discuss simulation results for cost of charging batteries for a week in summer and winter months. Also, with the smart grid implemented, we can calculate the cost discharging energy from the electric vehicles to the grid. We optimize the simulation scenarios with various battery conditions implemented on the group of electric vehicles classified based upon their age.

4.1 Driving Cycle

It is well known, that the performance of electric vehicle is stochastic and depends on many random variables. We have to take into account this random behavior.
Fig. 4.1. Inputs for driving cycle, (a) Acceleration for 100 vehicles for total distance (b) Velocity for 100 vehicles for total distance

The inputs to the vehicle model are acceleration and velocity for the same trip travelled from 124 West Freistadt Road in Thiensville to 3200 North Cramer Street in Milwaukee in Fig. 3.4 with the random behavior for the driving conditions. As the trips are random, the whole trip is completed with different time segments, but the distance covered by each trip is the same.

The complete driving cycle includes constant velocity, constant acceleration and constant deceleration cycles. There are 16 segments which form a complete driving cycle.
We have used same configuration of the electric vehicle as mentioned in Table 3.1.

4.2 Electricity Cost

In the smart grid systems, the cost of electricity varies during the 24 hour period of the day, and 365 days of the year. We also have the advantage to sell the energy and use the energy as per our convenience.
Fig. 4.2. Average energy requirement and cost for a week in summer, (a) Average energy cost for a week in summer, (b) Average energy requirement for a week in summer. (www.midwestiso.org)

The average cost of energy and amount of energy on the grid is represented as shown in Fig. 4.2. We observe the cost of energy during the nights is quite low compared to the cost of energy during the day time. The cost of energy from 12:00-7:00 AM is very less compared to the peak hours i.e. from 7:00AM to 7:00PM. There is deviation in the prices of energy and energy requirements on a daily basis.
We can clearly observe that there is deviation in the prices of energy on daily basis. The price of electricity on Monday 30\textsuperscript{th} July 2012 was $95.78 and at the same time on Tuesday 31\textsuperscript{st} 2012 was $35.09. Thus there is almost $60 difference in 2 consecutive days for the same hours of energy requirement. This makes it essential to know the correct times of charging and discharging of electric vehicles so that the operation is cost efficient.
efficient. Similarly, data about winter would help us to know the behavior of the energy on the grid.
Fig. 4.4. Average energy requirement and cost for a week in winter, (a) Average energy cost for a week in winter, (b) Average energy requirement for a week in winter
Fig. 4.5. (a) Energy price per hour on daily basis for a week in winter, (b) Energy requirement for a week on daily basis in winter.
We can observe in Fig. 4.4 (a) that the average cost for the whole week is in the range ~$10-15. But when we see the cost difference on a daily basis, we see that there are two hours on Monday 9\textsuperscript{th} Jan 2012 during which the cost is below zero which indicates that the user earns money for using energy from the grid. The negative cost is due to the cost associated with the minimum energy on the grid and the variable energy required on the grid.

The striking difference when we compare Fig. 4.4 and Fig. 4.5 is that the peak hours when the energy cost is at highest varies with the specific time of the day. During summers, the highest energy cost is at the end of the day from 3:00-7:00 PM where as the highest price of energy during winter months at the beginning of the day from 7:00 AM-12:00 PM.
4.3 Battery Charging Configuration

The battery internal resistance rises with its age and the pattern of usage. It does not increase overnight, but increases gradually on regular usage. There are many factors which contribute to the rise in the internal resistance like usage over a period of time, deep discharge cycles, various uncertainties, variable current input and output requirements etc. The internal resistance values used in this research are approximately equivalent to the lithium ion batteries of Chevrolet Volt. We assume that the increase in internal resistance is over the life of the battery.

Table 4.1. Battery internal resistance as per the age of battery during discharging

<table>
<thead>
<tr>
<th>Name</th>
<th>Battery Age (years)</th>
<th>Internal Resistance (Ω)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group 1</td>
<td>0-1.5</td>
<td>0.104</td>
</tr>
<tr>
<td>Group 2</td>
<td>1.5-3.0</td>
<td>0.156</td>
</tr>
<tr>
<td>Group 3</td>
<td>3.0-4.5</td>
<td>0.313</td>
</tr>
<tr>
<td>Group 4</td>
<td>4.5-6.0</td>
<td>0.521</td>
</tr>
</tbody>
</table>

We assume that the battery life for 6 years in this study that does not imply that the battery is not usable after 6 years. We just intend to study its performance through its working life. We assume that batteries are charged from 30% to 80% SOC on a daily basis. We assume that batteries are at 80% SOC at the beginning of the day i.e. at 7:00AM and it returns to 30% at the end of the day i.e. at 7:00 PM. The battery starts charging from 7:00 PM and is completely charged by 7:00 AM the next morning.
The charging times for electric vehicles change with their age. The charging times for vehicles depend on battery models. We use the battery model mentioned in Fig. 3.1, and Eq. 3.2 gives the SOC of the battery during charging.

![Charging Time for Batteries in All Groups](image)

**Fig. 4.6. Charging time for batteries in all the groups**

We consider that at the beginning of the charging cycle, the battery is at 30% SOC which is lowest for the operational range and when the battery is fully charged, we have 80% SOC on the battery for a full charged battery.

The charge process from grid for all batteries in the group is shown as in Fig. 4.6. The charging time increases as the internal resistance of the battery increases. The batteries are charged with 240V and 30A current until 60% SOC and then at 120V and 15A. The
charging pattern is selected to maintain battery health and performance. It can be seen that Group 1 battery charges in 4.74 hours, Group 2 requires 7.15 hours, Group 3 requires 9.0 hours and Group 4 requires 10.05 hours of charging.

From the driving cycle and the charging time required for charging of batteries, we can conclude that Group-4 batteries require maximum amount of charging time which increases the cost of charging also, Group 4 batteries require maximum amount of energy to complete a given trip, whereas Group 1 batteries require minimum amount of time for charging and require minimum percentage of SOC on the battery to complete the trip. Hence, cost for the trip would be minimized if we charge the battery at cheapest hour price.

With the advances in forecasting methods we can predict the day-ahead prices of the energy on the grid. We can certainly minimize the cost of charging knowing ahead of time the price of the energy. We know the amount of energy required by our vehicle and the price of energy available on the grid, this helps us to initiate charging only when the prices are lowest.

In the smart grid scenario, we can not only minimize the charging costs of the electric and plug-in hybrid vehicles, but also minimize the travel cost by exchanging the energy with the grid at the highest possible price to minimize the cost of the trip travelled.
4.4 Battery Discharging Configuration

We assume that there are 100 vehicles in each of the 4 battery groups. All batteries are charged from 30 to 80% SOC. The driving trips for 100 vehicles from each group are as shown in Fig. 4.1. The acceleration for 100 vehicles is as shown in Fig. 4.1(a) and velocity for the same is Fig. 4.1(b). The motor speed and torque profiles are as shown in Fig. 3.5.
Fig. 4.7. Battery performance: (a) Group 1 batteries, (b) Group 2 batteries, (c) Group 3 batteries, (d) Group 4 batteries

The whole driving cycle is converted into spatial mode as different segments take different amount of time but the distance remains constant. We drive 100 driving cycles with 4 battery configurations as mentioned in Table 4.1.

The driving distance for all the batteries is same but the energy required is different as the battery performance changes with the driving pattern and energy consumed by aged battery is more. We see that Group-1 batteries require average of 14.79% SOC with a standard deviation 0.325, Group-2 batteries require average of 15.55% SOC with a standard deviation of 0.31, Group-3 batteries require average of 16.8% SOC with a
standard deviation of 0.31, Group-4 batteries require average of 18.28% SOC with a standard deviation of 0.34 to complete the trip.
4.5 Optimizing Trip Cost

We consider day-ahead prices for charging the electric vehicles, the power supplied and power available for exchange from the electric vehicles is known. We assume to have 100 vehicles from each group for charging and exchange, so total number of vehicles taking part in the simulation study is 400. The objective function for the study is

\[
\text{Cost} = \max \sum_{i=1}^{24} [(p_{b5i} \cdot C_i \cdot x_5 + p_{b6i} \cdot C_i \cdot x_6 + p_{b7i} \cdot C_i \cdot x_7 + p_{b8i} \cdot C_i \cdot x_8) - (p_{b1i} \cdot C_i \cdot x_1 + p_{b2i} \cdot C_i \cdot x_2 + p_{b3i} \cdot C_i \cdot x_3 + p_{b4i} \cdot C_i \cdot x_4)]
\]  

(4.1)

where,

- \( C_i \) is the energy cost per hour
- \( p_{b1i} \) is the battery energy in any specific hour from Group-1
- \( p_{b2i} \) is the battery energy in any specific hour from Group-2
- \( p_{b3i} \) is the battery energy in any specific hour from Group-3
- \( p_{b4i} \) is the battery energy in any specific hour from Group-4
- \( p_{b5i} \) is the battery energy exchanged with the grid at any specific hour from Group-1
- \( p_{b6i} \) is the battery energy exchanged with the grid at any specific hour from Group-2
- \( p_{b7i} \) is the battery energy exchanged with the grid at any specific hour from Group-3
- \( p_{b8i} \) is the battery energy exchanged with the grid at any specific hour from Group-4
- \( x_5 \) is the energy given to the grid at any specific hour
- \( x_6 \) is the energy given to the grid at any specific hour
- \( x_7 \) is the energy given to the grid at any specific hour
- \( x_8 \) is the energy given to the grid at any specific hour
- \( x_1-x_4 \) is the number of batteries connected to the grid from group 1 to 4 respectively
4.6 Opportunity Cost

We assume that we have the knowledge of the cost of charging and cost of discharging on a specific day of the week. This knowledge provides us the cost of energy on the specific day for which we estimate the charging discharging pattern. We define opportunity cost as

\[
\text{Opportunity Cost} = \frac{\text{Cost Spent on Charging} \ (\$/KWh)}{\text{Cost Earned with Exchanging} \ (\$/KWh)}
\]  

(4.2)

To derive the opportunity cost, we require the average cost for charging of batteries from group 1 to group 4 and money earned with exchanging energy to the grid from group 5 to group 8 batteries. Batteries from group 1 to group 4 are assumed to have 16.5KWh of onboard energy when they are completely charged. Batteries from group 5 to group 8 have varied energy for exchange. Opportunity Cost would be a measure to evaluate the performance of a particular group of batteries on a specific day for which we forecast the price of charging and have knowledge of the trip we are planning to travel.
4.7 Optimized Battery Cycles

Case 1:

All the batteries are available for exchange at any point of the day. As we charge all the batteries to 80% SOC and use these batteries for the driving cycle. We have knowledge of the energy available for exchange from all the batteries i.e. Group 1 to Group 4.

Table 4.2. Battery energy capacity available for exchange

<table>
<thead>
<tr>
<th>Name</th>
<th>Battery Age (years)</th>
<th>Energy (KWh)/EV</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group 5</td>
<td>0-1.5</td>
<td>6.25</td>
</tr>
<tr>
<td>Group 6</td>
<td>1.5-3.0</td>
<td>5.88</td>
</tr>
<tr>
<td>Group 7</td>
<td>3.0-4.5</td>
<td>4.99</td>
</tr>
<tr>
<td>Group 8</td>
<td>4.5-6.0</td>
<td>3.88</td>
</tr>
</tbody>
</table>

The energy available for exchanging with the grid is as shown in Table 4.2. The energy supplied for charging is known which is as given in Fig. 4.6. We get the optimized cost of the trip with the specific energy used for charging and selling the energy at the highest cost during driving day. We use cost for the energy from the Midwest Independent Transmission System Operator [35].
We have access to all the batteries for all the hours after charging which results in the trip cost for 400 vehicles as $195,822.

Fig. 4.8. Batteries performance connected to grid
Case 2:

We assume that we have limited number of batteries for exchange for every hour from all the groups. We limit the batteries we can connect to the grid at any point to 15 from each group. We have energy available for exchange as given in Table 4.2.

![Fig. 4.9. Number of batteries connected to grid](image)

The cost function when we have limited batteries to connect with the grid and supply energy, we get the cost of charging as $217.805. We observe that 15 batteries from each
group are connected at first 6 highest cost hours and the remaining 10 batteries from each group are connected at the next highest cost.

**Case 3:**

In this case we limit the maximum energy, the user can trades with the grid. We assume that the energy requirement of the grid is maximum 450KWh at any hour of the day. The data we simulate is for a week in summer i.e. from 7/30/2012 (Monday) to 8/3/2012 (Friday).

![Graph showing number of electric vehicles charging and energy exchanged with grid](image-url)
Fig. 4.10. Performance of batteries during a week in summer, (a) Monday cycle, (b) Tuesday cycle, (c) Wednesday cycle, (d) Thursday cycle, (e) Friday cycle.
We use Matlab Linprog function to simulate our data and find the optimized cost of charging of the batteries of all groups. We study the charging of batteries and discharging of batteries for a week in summer 2012. We assume that our battery cycle begins 7:00pm and is completed at 7:00pm the next day. We assume batteries charge from 7:00pm to 7:00am. The batteries are assumed to be at 30% SOC with the beginning of the charging cycle. Total numbers of batteries which are connected for charging from 7:00pm to 7:00am are represented by group-1 to group-4 in Fig. 4.10. The amount of energy the batteries exchange with the grid at any hour from 7:00am to 7:00pm is given by group-5 to group-8 in Fig. 4.10.

Table 4.3. Cost of battery cycle per day in summer

<table>
<thead>
<tr>
<th></th>
<th>Monday</th>
<th>Tuesday</th>
<th>Wednesday</th>
<th>Thursday</th>
<th>Friday</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Cost Function</strong></td>
<td>149.0338</td>
<td>229.5838</td>
<td>158.1974</td>
<td>246.4039</td>
<td>231.92</td>
</tr>
</tbody>
</table>

The total cost of battery cycle to the user for a weekday is shown as in Table 4.3. We also know the cost of charging and exchanging energy to the grid.
We calculate the total cost of charging batteries from each group-1 to group-4. Then we also calculate the money earned by exchanging available energy in the batteries with the grid. Thus we have the estimated costs of energy per kilowatt in charging and discharging to the grid. The cost for group-1 to group-8 is as shown in Fig. 4.11.

In Fig. 4.11 we can see that group-1 to group-4 is the average performance of batteries during charging whereas group-5 to group-8 is the average performance to the batteries
during exchange. Group-5 consists to batteries from group-1 during exchange, group-6 consist batteries from group-2 during exchange, group-7 consists batteries from group-3 during exchange and group-8 consists batteries from group-8 during exchange.

Table 4.4. Opportunity cost for Week in summer

<table>
<thead>
<tr>
<th></th>
<th>Monday</th>
<th>Tuesday</th>
<th>Wednesday</th>
<th>Thursday</th>
<th>Friday</th>
</tr>
</thead>
<tbody>
<tr>
<td>OCB-1</td>
<td>0.266788</td>
<td>0.657697</td>
<td>0.330647</td>
<td>0.703908</td>
<td>0.544808</td>
</tr>
<tr>
<td>OCB-2</td>
<td>0.464569</td>
<td>1.033423</td>
<td>0.512832</td>
<td>1.062479</td>
<td>0.901849</td>
</tr>
<tr>
<td>OCB-3</td>
<td>0.699473</td>
<td>1.349427</td>
<td>0.697043</td>
<td>1.364664</td>
<td>1.217155</td>
</tr>
<tr>
<td>OCB-4</td>
<td>1.032016</td>
<td>1.710461</td>
<td>0.946929</td>
<td>1.759759</td>
<td>1.607286</td>
</tr>
</tbody>
</table>

We calculate the opportunity cost from equation 18. The opportunity cost indicates the amount of profit. It is clear from the opportunity cost function that smaller the opportunity cost, greater is the profit. Opportunity cost greater than 1 indicates that we spent more on charging the batteries than we earn in exchanging energy to the grid. We can observe in Table 4.4 that on Monday the opportunity cost for battery-4 is greater than 1 which indicates that the cost or charging the batteries is higher than the cost of energy exchanged from the batteries to the grid. On Tuesday the opportunity cost for Battery-2, Battery-3 and Battery-4 is greater than 1, similarly, on Thursday the opportunity cost for Battery-2 Battery-3 and Battery-4 is greater than 1 and on Friday the opportunity cost for Battery-3 and Battery-4 are greater than 1. These all cases indicate that the opportunity cost is greater than 1 and the cost of charging is greater than the money earned from selling energy from the electric vehicles to the grid. Whereas on Wednesday the
opportunity cost of Battery-1, Battery-2, Battery-3 and Battery-4 are less than 1 which indicates profit from selling the energy to the grid.
Case 4:

We use a similar analysis as in Case-3 to simulate a week’s data during winter i.e. from 01/09/2012 to 01/13/2012 (Monday to Friday). We limit the energy requirement from the grid to 450KWh.
Fig. 4.12. Performance of batteries during a week in winter, (a) Monday cycle, (b) Tuesday cycle, (c) Wednesday cycle, (d) Thursday cycle, (e) Friday Cycle
We use Matlab linear programming (\textit{linprog}) function for evaluating the hours of the day when the battery is connected to the grid and cost of charging of electric vehicles. The simulation results for a week in winter help us to understand the load distribution of the electric vehicles on the grid. It also helps to understand the exact period which is beneficial to the user to connect the electric vehicles to support the grid so that the user earns maximum profit. We charge the batteries from 7.00pm to 7.00am. The batteries completely discharge from 7:00am to 7:00pm. They complete the driving cycle and then exchange the excess energy with the grid. These batteries are available for exchange anytime of the day and the grid requirement is set to maximum to maximum of 450KWh of energy needed in any day.

Table 4.5. Cost of battery cycle per day in winter

<table>
<thead>
<tr>
<th></th>
<th>Monday</th>
<th>Tuesday</th>
<th>Wednesday</th>
<th>Thursday</th>
<th>Friday</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Cost Function</strong></td>
<td>67.326</td>
<td>229.545</td>
<td>207.572</td>
<td>206.7455</td>
<td>278.5981</td>
</tr>
</tbody>
</table>

We get the cost functions for weekdays for a week in winter as given in Table 4.5. The cost value comprises of charging cost and the grid exchange cost.
Fig. 4.13. Costs incurred and gained during charging and exchanging energy with grid in winter

From Fig. 4.13, we can estimate the cost of charging from the cost values of group 1 to group 4 during a week. We know the cost of exchanging energy with the grid from the cost values of group 5 to group 8. We calculate the opportunity cost as given in equation 6. Group-1 to group-4 is the average performance of batteries during charging per hour whereas group-5 to group-8 is the average performance to the batteries during exchange to the grid per hour. Group-5 consists to batteries from group-1 during exchange, group-6
consist batteries from group-2 during exchange, group-7 consists batteries from group-3 during exchange and group-8 consists batteries from group-4 during exchange.

Table 4.6. Opportunity Cost for a week in winter

<table>
<thead>
<tr>
<th></th>
<th>Monday</th>
<th>Tuesday</th>
<th>Wednesday</th>
<th>Thursday</th>
<th>Friday</th>
</tr>
</thead>
<tbody>
<tr>
<td>OCB-1</td>
<td>0.030171</td>
<td>0.690971</td>
<td>0.902569</td>
<td>0.773916</td>
<td>0.763186</td>
</tr>
<tr>
<td>OCB-2</td>
<td>0.328167</td>
<td>1.030022</td>
<td>1.407692</td>
<td>1.302486</td>
<td>1.158731</td>
</tr>
<tr>
<td>OCB-3</td>
<td>0.79132</td>
<td>1.256656</td>
<td>1.715464</td>
<td>1.822246</td>
<td>1.478382</td>
</tr>
<tr>
<td>OCB-4</td>
<td>1.26712</td>
<td>1.506383</td>
<td>2.140395</td>
<td>2.430348</td>
<td>1.802676</td>
</tr>
</tbody>
</table>

Thus from Table 4.4 and Table 4.6, we can clearly observe that there are cases for battery group’s where we are at a loss charging the batteries to 80% of SOC. We intend to reduce the cost of charging by charging the batteries only to cater the trip in the cases where loss is registered. We observe from Table 4.6 that opportunity costs for Battery-1, Battery-2, Battery-3 and Battery-4 is greater than 1 from Tuesday to Friday of the week, whereas the opportunity cost for Battery-4 is greater than 1. The opportunity costs for batteries less than 1 indicate profit by exchanging energy from the user to the grid. Our intention is to reduce the battery cycle cost by reducing the energy level on the battery which facilitates charging batteries to lower energy level.
5. Conclusions and Recommendations

In this study, we proposed a metric to determine the worthiness of replacement (WOR) for the battery. This idea was successfully demonstrated with two module and three module systems. We can conclude from the simulation that with drop in SOC and increase in internal resistance, battery performance decreases during a driving cycle. As the WOR number increases, the battery tends to be more prone to replacement. Though we work in acceptable limits of the battery in our simulation study, there is a considerable loss of energy due to the internal resistance of low energy cell. If a worse battery is considered for that matter, the battery would run out of energy during a driving cycle and the trip will be incomplete. Thus with the knowledge of the health map, we could exactly specify whether the onboard energy can complete the trip successfully. It is completely a user’s choice to opt for replacement of the poor cell, as the user only has the knowledge of his trip and the performance of the batteries. We introduce an index so that the user makes his decision for replacement based the cost of battery, labor and overall utility requirements.

As the battery performance degrades over its life time, it takes more time for charging. As the time for charging increases, the charging cost also will increase. The batteries also use more energy compared to the performance of the batteries when they are new. This adds on to the cost of driving the trip. With the optimization of the charging and discharging cycles based on the battery health, we can minimize the cost of trip traveled. We exploit the smart grid system to balance the energy requirement and provide advantage to the user of the opportunity for exchange of energy with the grid. The
knowledge of the price of energy and the quantity of energy required by the trip enables us to establish for our pattern of charging and discharging cycles.

Our future research is to consider cases with degraded cells and consider the battery behavior more rigorously. Also we tend to model the behavior of the internal resistance with various cases during the driving cycle. We intend to know the state of charge of batteries based on the internal resistance map. Also, we will aim to judge the charging patterns for each battery and to limit the state of charge (SOC) of the batteries so as to minimize the cost of trip and maximize our profit when energy is exchanged with grid.
References


35. www.midwestiso.org

[https://www.midwestiso.org/Library/MarketReports/Pages/MarketReports.aspx]